

# NAG Fortran Library

## Mark 20 Library Contents

### A00 – Library Identification

A00AAF Prints details of the NAG Fortran Library implementation

### A02 – Complex Arithmetic

A02AAF Square root of complex number  
A02ABF Modulus of complex number  
A02ACF Quotient of two complex numbers

### C02 – Zeros of Polynomials

C02AFF All zeros of complex polynomial, modified Laguerre method  
C02AGF All zeros of real polynomial, modified Laguerre method  
C02AHF All zeros of complex quadratic equation  
C02AJF All zeros of real quadratic equation  
C02AKF All zeros of real cubic equation  
C02ALF All zeros of real quartic equation  
C02AMF All zeros of complex cubic equation  
C02ANF All zeros of complex quartic equation

### C05 – Roots of One or More Transcendental Equations

C05ADF Zero of continuous function in given interval, Bus and Dekker algorithm  
C05AGF Zero of continuous function, Bus and Dekker algorithm, from given starting value, binary search for interval  
C05AJF Zero of continuous function, continuation method, from a given starting value  
C05AVF Binary search for interval containing zero of continuous function (reverse communication)  
C05AXF Zero of continuous function by continuation method, from given starting value (reverse communication)  
C05AZF Zero in given interval of continuous function by Bus and Dekker algorithm (reverse communication)  
C05NBF Solution of system of nonlinear equations using function values only (easy-to-use)  
C05NCF Solution of system of nonlinear equations using function values only (comprehensive)  
C05NDF Solution of system of nonlinear equations using function values only (reverse communication)  
C05PBF Solution of system of nonlinear equations using first derivatives (easy-to-use)  
C05PCF Solution of system of nonlinear equations using first derivatives (comprehensive)  
C05PDF Solution of system of nonlinear equations using first derivatives (reverse communication)  
C05ZAF Check user's routine for calculating first derivatives

### C06 – Summation of Series

C06BAF Acceleration of convergence of sequence, Shanks' transformation and epsilon algorithm  
C06DBF Sum of a Chebyshev series  
C06EAF Single one-dimensional real discrete Fourier transform, no extra workspace  
C06EBF Single one-dimensional Hermitian discrete Fourier transform, no extra workspace  
C06ECF Single one-dimensional complex discrete Fourier transform, no extra workspace  
C06EKF Circular convolution or correlation of two real vectors, no extra workspace  
C06FAF Single one-dimensional real discrete Fourier transform, extra workspace for greater speed  
C06FBF Single one-dimensional Hermitian discrete Fourier transform, extra workspace for greater speed  
C06FCF Single one-dimensional complex discrete Fourier transform, extra workspace for greater speed  
C06FFF One-dimensional complex discrete Fourier transform of multi-dimensional data  
C06FJF Multi-dimensional complex discrete Fourier transform of multi-dimensional data  
C06FKF Circular convolution or correlation of two real vectors, extra workspace for greater speed  
C06FPF Multiple one-dimensional real discrete Fourier transforms

|        |  |
|--------|--|
| C06FQF | Multiple one-dimensional Hermitian discrete Fourier transforms   |
| C06FRF | Multiple one-dimensional complex discrete Fourier transforms   |
| C06FUF | Two-dimensional complex discrete Fourier transform   |
| C06FXF | Three-dimensional complex discrete Fourier transform   |
| C06GBF | Complex conjugate of Hermitian sequence  |
| C06GCF | Complex conjugate of complex sequence  |
| C06GQF | Complex conjugate of multiple Hermitian sequences  |
| C06GSF | Convert Hermitian sequences to general complex sequences   |
| C06HAF | Discrete sine transform  |
| C06HBF | Discrete cosine transform  |
| C06HCF | Discrete quarter-wave sine transform   |
| C06HDF | Discrete quarter-wave cosine transform   |
| C06LAF | Inverse Laplace transform, Crump's method  |
| C06LBF | Inverse Laplace transform, modified Weeks' method  |
| C06LCF | Evaluate inverse Laplace transform as computed by C06LBF   |
| C06PAF | Single one-dimensional real and Hermitian complex discrete Fourier transform, using complex data format for Hermitian sequences    |
| C06PCF | Single one-dimensional complex discrete Fourier transform, complex data format   |
| C06PFF | One-dimensional complex discrete Fourier transform of multi-dimensional data (using complex data type)                             |
| C06PJF | Multi-dimensional complex discrete Fourier transform of multi-dimensional data (using complex data type)                           |
| C06PKF | Circular convolution or correlation of two complex vectors   |
| C06PPF | Multiple one-dimensional real and Hermitian complex discrete Fourier transforms, using complex data format for Hermitian sequences |
| C06PQF | Multiple one-dimensional real and Hermitian complex discrete Fourier transforms, using complex data format for Hermitian sequences |
| C06PRF | Multiple one-dimensional complex discrete Fourier transforms using complex data format   |
| C06PSF | Multiple one-dimensional complex discrete Fourier transforms using complex data format and sequences stored as columns             |
| C06PUF | Two-dimensional complex discrete Fourier transform, complex data format  |
| C06PXF | Three-dimensional complex discrete Fourier transform, complex data format  |
| C06RAF | Discrete sine transform (easy-to-use)  |
| C06RBF | Discrete cosine transform (easy-to-use)  |
| C06RCF | Discrete quarter-wave sine transform (easy-to-use)   |
| C06RDF | Discrete quarter-wave cosine transform (easy-to-use)   |

## D01 – Quadrature

|        |   |
|--------|---|
| D01AHF | One-dimensional quadrature, adaptive, finite interval, strategy due to Patterson, suitable for well-behaved integrands                |
| D01AJF | One-dimensional quadrature, adaptive, finite interval, strategy due to Piessens and de Doncker, allowing for badly-behaved integrands |
| D01AKF | One-dimensional quadrature, adaptive, finite interval, method suitable for oscillating functions                                      |
| D01ALF | One-dimensional quadrature, adaptive, finite interval, allowing for singularities at user-specified break-points                      |
| D01AMF | One-dimensional quadrature, adaptive, infinite or semi-infinite interval  |
| D01ANF | One-dimensional quadrature, adaptive, finite interval, weight function $\cos(\omega x)$ or $\sin(\omega x)$                           |
| D01APF | One-dimensional quadrature, adaptive, finite interval, weight function with end-point singularities of algebraico-logarithmic type    |
| D01AQF | One-dimensional quadrature, adaptive, finite interval, weight function $1/(x - c)$ , Cauchy principal value (Hilbert transform)       |
| D01ARF | One-dimensional quadrature, non-adaptive, finite interval with provision for indefinite integrals                                     |
| D01ASF | One-dimensional quadrature, adaptive, semi-infinite interval, weight function $\cos(\omega x)$ or $\sin(\omega x)$                    |
| D01ATF | One-dimensional quadrature, adaptive, finite interval, variant of D01AJF efficient on vector machines                                 |
| D01AUF | One-dimensional quadrature, adaptive, finite interval, variant of D01AKF efficient on vector machines                                 |
| D01BAF | One-dimensional Gaussian quadrature   |

|        |   |
|--------|---|
| D01BBF | Pre-computed weights and abscissae for Gaussian quadrature rules, restricted choice of rule                                   |
| D01BCF | Calculation of weights and abscissae for Gaussian quadrature rules, general choice of rule                                    |
| D01BDF | One-dimensional quadrature, non-adaptive, finite interval   |
| D01DAF | Two-dimensional quadrature, finite region   |
| D01EAF | Multi-dimensional adaptive quadrature over hyper-rectangle, multiple integrands   |
| D01FBF | Multi-dimensional Gaussian quadrature over hyper-rectangle  |
| D01FCF | Multi-dimensional adaptive quadrature over hyper-rectangle  |
| D01FDF | Multi-dimensional quadrature, Sag–Szekeres method, general product region or $n$ -sphere                                      |
| D01GAF | One-dimensional quadrature, integration of function defined by data values, Gill–Miller method                                |
| D01GBF | Multi-dimensional quadrature over hyper-rectangle, Monte Carlo method   |
| D01GCF | Multi-dimensional quadrature, general product region, number-theoretic method   |
| D01GDF | Multi-dimensional quadrature, general product region, number-theoretic method, variant of D01GCF efficient on vector machines |
| D01GYF | Korobov optimal coefficients for use in D01GCF or D01GDF, when number of points is prime                                      |
| D01GZF | Korobov optimal coefficients for use in D01GCF or D01GDF, when number of points is product of two primes                      |
| D01JAF | Multi-dimensional quadrature over an $n$ -sphere, allowing for badly-behaved integrands                                       |
| D01PAF | Multi-dimensional quadrature over an $n$ -simplex   |

## D02 – Ordinary Differential Equations

|        |   |
|--------|---|
| D02AGF | ODEs, boundary value problem, shooting and matching technique, allowing interior matching point, general parameters to be determined            |
| D02BGF | ODEs, IVP, Runge–Kutta–Merson method, until a component attains given value (simple driver)   |
| D02BHF | ODEs, IVP, Runge–Kutta–Merson method, until function of solution is zero (simple driver)  |
| D02BJF | ODEs, IVP, Runge–Kutta method, until function of solution is zero, integration over range with intermediate output (simple driver)              |
| D02CJF | ODEs, IVP, Adams method, until function of solution is zero, intermediate output (simple driver)  |
| D02EJF | ODEs, stiff IVP, BDF method, until function of solution is zero, intermediate output (simple driver)  |
| D02GAF | ODEs, boundary value problem, finite difference technique with deferred correction, simple nonlinear problem                                    |
| D02GBF | ODEs, boundary value problem, finite difference technique with deferred correction, general linear problem                                      |
| D02HAF | ODEs, boundary value problem, shooting and matching, boundary values to be determined   |
| D02HBF | ODEs, boundary value problem, shooting and matching, general parameters to be determined  |
| D02JAF | ODEs, boundary value problem, collocation and least-squares, single $n$ th-order linear equation  |
| D02JBF | ODEs, boundary value problem, collocation and least-squares, system of first-order linear equations   |
| D02KAF | Second-order Sturm–Liouville problem, regular system, finite range, eigenvalue only   |
| D02KDF | Second-order Sturm–Liouville problem, regular/singular system, finite/infinite range, eigenvalue only, user-specified break-points              |
| D02KEF | Second-order Sturm–Liouville problem, regular/singular system, finite/infinite range, eigenvalue and eigenfunction, user-specified break-points |
| D02LAF | Second-order ODEs, IVP, Runge–Kutta–Nystrom method  |
| D02LXF | Second-order ODEs, IVP, setup for D02LAF  |
| D02LYF | Second-order ODEs, IVP, diagnostics for D02LAF  |
| D02LZF | Second-order ODEs, IVP, interpolation for D02LAF  |
| D02MVF | ODEs, IVP, DASSL method, setup for D02M–N routines  |
| D02MZF | ODEs, IVP, interpolation for D02M–N routines, natural interpolant   |
| D02NBF | Explicit ODEs, stiff IVP, full Jacobian (comprehensive)   |
| D02NCF | Explicit ODEs, stiff IVP, banded Jacobian (comprehensive)   |
| D02NDF | Explicit ODEs, stiff IVP, sparse Jacobian (comprehensive)   |
| D02NGF | Implicit/algebraic ODEs, stiff IVP, full Jacobian (comprehensive)   |
| D02NHF | Implicit/algebraic ODEs, stiff IVP, banded Jacobian (comprehensive)   |
| D02NJF | Implicit/algebraic ODEs, stiff IVP, sparse Jacobian (comprehensive)   |
| D02NMF | Explicit ODEs, stiff IVP (reverse communication, comprehensive)   |
| D02NNF | Implicit/algebraic ODEs, stiff IVP (reverse communication, comprehensive)   |

|        |  |
|--------|--|
| D02NRF | ODEs, IVP, for use with D02M–N routines, sparse Jacobian, enquiry routine  |
| D02NSF | ODEs, IVP, for use with D02M–N routines, full Jacobian, linear algebra set up  |
| D02NTF | ODEs, IVP, for use with D02M–N routines, banded Jacobian, linear algebra set up  |
| D02NUF | ODEs, IVP, for use with D02M–N routines, sparse Jacobian, linear algebra set up  |
| D02NVF | ODEs, IVP, BDF method, setup for D02M–N routines   |
| D02NWF | ODEs, IVP, Blend method, setup for D02M–N routines   |
| D02NXF | ODEs, IVP, sparse Jacobian, linear algebra diagnostics, for use with D02M–N routines   |
| D02NYF | ODEs, IVP, integrator diagnostics, for use with D02M–N routines  |
| D02NZF | ODEs, IVP, setup for continuation calls to integrator, for use with D02M–N routines  |
| D02PCF | ODEs, IVP, Runge–Kutta method, integration over range with output  |
| D02PDF | ODEs, IVP, Runge–Kutta method, integration over one step   |
| D02PVF | ODEs, IVP, setup for D02PCF and D02PDF   |
| D02PWF | ODEs, IVP, resets end of range for D02PDF  |
| D02PXF | ODEs, IVP, interpolation for D02PDF  |
| D02PYF | ODEs, IVP, integration diagnostics for D02PCF and D02PDF   |
| D02PZF | ODEs, IVP, error assessment diagnostics for D02PCF and D02PDF  |
| D02QFF | ODEs, IVP, Adams method with root-finding (forward communication, comprehensive)   |
| D02QGF | ODEs, IVP, Adams method with root-finding (reverse communication, comprehensive)   |
| D02QWF | ODEs, IVP, setup for D02QFF and D02QGF   |
| D02QXF | ODEs, IVP, diagnostics for D02QFF and D02QGF   |
| D02QYF | ODEs, IVP, root-finding diagnostics for D02QFF and D02QGF  |
| D02QZF | ODEs, IVP, interpolation for D02QFF or D02QGF  |
| D02RAF | ODEs, general nonlinear boundary value problem, finite difference technique with deferred correction, continuation facility              |
| D02SAF | ODEs, boundary value problem, shooting and matching technique, subject to extra algebraic equations, general parameters to be determined |
| D02TGF | $n$ th-order linear ODEs, boundary value problem, collocation and least-squares  |
| D02TKF | ODEs, general nonlinear boundary value problem, collocation technique  |
| D02TVF | ODEs, general nonlinear boundary value problem, setup for D02TKF   |
| D02TXF | ODEs, general nonlinear boundary value problem, continuation facility for D02TKF   |
| D02TYF | ODEs, general nonlinear boundary value problem, interpolation for D02TKF   |
| D02TZF | ODEs, general nonlinear boundary value problem, diagnostics for D02TKF   |
| D02XJF | ODEs, IVP, interpolation for D02M–N routines, natural interpolant  |
| D02XKF | ODEs, IVP, interpolation for D02M–N routines, $C_1$ interpolant  |
| D02ZAF | ODEs, IVP, weighted norm of local error estimate for D02M–N routines   |

### D03 – Partial Differential Equations

|        |  |
|--------|--|
| D03EAF | Elliptic PDE, Laplace's equation, two-dimensional arbitrary domain   |
| D03EBF | Elliptic PDE, solution of finite difference equations by SIP, five-point two-dimensional molecule, iterate to convergence  |
| D03ECF | Elliptic PDE, solution of finite difference equations by SIP for seven-point three-dimensional molecule, iterate to convergence  |
| D03EDF | Elliptic PDE, solution of finite difference equations by a multigrid technique   |
| D03EEF | Discretize a second-order elliptic PDE on a rectangle  |
| D03FAF | Elliptic PDE, Helmholtz equation, three-dimensional Cartesian co-ordinates   |
| D03MAF | Triangulation of plane region  |
| D03NCF | Finite difference solution of the Black–Scholes equations  |
| D03NDF | Analytic solution of the Black–Scholes equations   |
| D03NEF | Compute average values for D03NDF  |
| D03PCF | General system of parabolic PDEs, method of lines, finite differences, one space variable  |
| D03PDF | General system of parabolic PDEs, method of lines, Chebyshev $C^0$ collocation, one space variable   |
| D03PEF | General system of first-order PDEs, method of lines, Keller box discretisation, one space variable   |
| D03PFF | General system of convection-diffusion PDEs with source terms in conservative form, method of lines, upwind scheme using numerical flux function based on Riemann solver, one space variable |

- D03PHF General system of parabolic PDEs, coupled DAEs, method of lines, finite differences, one space variable
- D03PJF General system of parabolic PDEs, coupled DAEs, method of lines, Chebyshev  $C^0$  collocation, one space variable
- D03PKF General system of first-order PDEs, coupled DAEs, method of lines, Keller box discretisation, one space variable
- D03PLF General system of convection-diffusion PDEs with source terms in conservative form, coupled DAEs, method of lines, upwind scheme using numerical flux function based on Riemann solver, one space variable
- D03PPF General system of parabolic PDEs, coupled DAEs, method of lines, finite differences, remeshing, one space variable
- D03PRF General system of first-order PDEs, coupled DAEs, method of lines, Keller box discretisation, remeshing, one space variable
- D03PSF General system of convection-diffusion PDEs with source terms in conservative form, coupled DAEs, method of lines, upwind scheme using numerical flux function based on Riemann solver, remeshing, one space variable
- D03PUF Roe's approximate Riemann solver for Euler equations in conservative form, for use with D03PFF, D03PLF and D03PSF
- D03PVF Osher's approximate Riemann solver for Euler equations in conservative form, for use with D03PFF, D03PLF and D03PSF
- D03PWF Modified HLL Riemann solver for Euler equations in conservative form, for use with D03PFF, D03PLF and D03PSF
- D03PXF Exact Riemann Solver for Euler equations in conservative form, for use with D03PFF, D03PLF and D03PSF
- D03PYF PDEs, spatial interpolation with D03PDF/D03PDA or D03PJF/D03PJA
- D03PZF PDEs, spatial interpolation with D03PCF/D03PCA, D03PEF, D03PFF, D03PHF/D03PHA, D03PKF, D03PLF, D03PPF/D03PPA, D03PRF or D03PSF
- D03RAF General system of second-order PDEs, method of lines, finite differences, remeshing, two space variables, rectangular region
- D03RBF General system of second-order PDEs, method of lines, finite differences, remeshing, two space variables, rectilinear region
- D03RYF Check initial grid data in D03RBF
- D03RZF Extract grid data from D03RBF
- D03UAF Elliptic PDE, solution of finite difference equations by SIP, five-point two-dimensional molecule, one iteration
- D03UBF Elliptic PDE, solution of finite difference equations by SIP, seven-point three-dimensional molecule, one iteration

## D04 – Numerical Differentiation

- D04AAF Numerical differentiation, derivatives up to order 14, function of one real variable

## D05 – Integral Equations

- D05AAF Linear non-singular Fredholm integral equation, second kind, split kernel
- D05ABF Linear non-singular Fredholm integral equation, second kind, smooth kernel
- D05BAF Nonlinear Volterra convolution equation, second kind
- D05BDF Nonlinear convolution Volterra–Abel equation, second kind, weakly singular
- D05BEF Nonlinear convolution Volterra–Abel equation, first kind, weakly singular
- D05BWF Generate weights for use in solving Volterra equations
- D05BYF Generate weights for use in solving weakly singular Abel-type equations

## D06 – Mesh Generation

- D06AAF Generates a two-dimensional mesh using a simple incremental method
- D06ABF Generates a two-dimensional mesh using a Delaunay–Voronoi process
- D06ACF Generates a two-dimensional mesh using an Advancing-front method
- D06BAF Generates a boundary mesh
- D06CAF Uses a barycentering technique to smooth a given mesh

D06CBF Generates a sparsity pattern of a Finite Element matrix associated with a given mesh  
 D06CCF Renumbers a given mesh using Gibbs method  
 D06DAF Generates a mesh resulting from an affine transformation of a given mesh  
 D06DBF Joins together two given adjacent (possibly overlapping) meshes

## E01 – Interpolation

E01AAF Interpolated values, Aitken's technique, unequally spaced data, one variable  
 E01ABF Interpolated values, Everett's formula, equally spaced data, one variable  
 E01AEF Interpolating functions, polynomial interpolant, data may include derivative values, one variable  
 E01BAF Interpolating functions, cubic spline interpolant, one variable  
 E01BEF Interpolating functions, monotonicity-preserving, piecewise cubic Hermite, one variable  
 E01BFF Interpolated values, interpolant computed by E01BEF, function only, one variable  
 E01BGF Interpolated values, interpolant computed by E01BEF, function and first derivative, one variable  
 E01BHF Interpolated values, interpolant computed by E01BEF, definite integral, one variable  
 E01DAF Interpolating functions, fitting bicubic spline, data on rectangular grid  
 E01RAF Interpolating functions, rational interpolant, one variable  
 E01RBF Interpolated values, evaluate rational interpolant computed by E01RAF, one variable  
 E01SAF Interpolating functions, method of Renka and Cline, two variables  
 E01SBF Interpolated values, evaluate interpolant computed by E01SAF, two variables  
 E01SGF Interpolating functions, modified Shepard's method, two variables  
 E01SHF Interpolated values, evaluate interpolant computed by E01SGF, function and first derivatives, two variables  
 E01TGF Interpolating functions, modified Shepard's method, three variables  
 E01THF Interpolated values, evaluate interpolant computed by E01TGF, function and first derivatives, three variables

## E02 – Curve and Surface Fitting

E02ACF Minimax curve fit by polynomials  
 E02ADF Least-squares curve fit, by polynomials, arbitrary data points  
 E02AEF Evaluation of fitted polynomial in one variable from Chebyshev series form (simplified parameter list)  
 E02AFF Least-squares polynomial fit, special data points (including interpolation)  
 E02AGF Least-squares polynomial fit, values and derivatives may be constrained, arbitrary data points  
 E02AHF Derivative of fitted polynomial in Chebyshev series form  
 E02AJF Integral of fitted polynomial in Chebyshev series form  
 E02AKF Evaluation of fitted polynomial in one variable from Chebyshev series form  
 E02BAF Least-squares curve cubic spline fit (including interpolation)  
 E02BBF Evaluation of fitted cubic spline, function only  
 E02BCF Evaluation of fitted cubic spline, function and derivatives  
 E02BDF Evaluation of fitted cubic spline, definite integral  
 E02BEF Least-squares cubic spline curve fit, automatic knot placement  
 E02CAF Least-squares surface fit by polynomials, data on lines  
 E02CBF Evaluation of fitted polynomial in two variables  
 E02DAF Least-squares surface fit, bicubic splines  
 E02DCF Least-squares surface fit by bicubic splines with automatic knot placement, data on rectangular grid  
 E02DDF Least-squares surface fit by bicubic splines with automatic knot placement, scattered data  
 E02DEF Evaluation of fitted bicubic spline at a vector of points  
 E02DFF Evaluation of fitted bicubic spline at a mesh of points  
 E02GAF  $L_1$ -approximation by general linear function  
 E02GBF  $L_1$ -approximation by general linear function subject to linear inequality constraints  
 E02GCF  $L_\infty$ -approximation by general linear function  
 E02RAF Padé-approximants  
 E02RBF Evaluation of fitted rational function as computed by E02RAF  
 E02ZAF Sort two-dimensional data into panels for fitting bicubic splines

**E04 – Minimizing or Maximizing a Function**

- E04ABF Minimum, function of one variable using function values only
- E04BBF Minimum, function of one variable, using first derivative
- E04CCF Unconstrained minimum, simplex algorithm, function of several variables using function values only (comprehensive)
- E04DGF Unconstrained minimum, preconditioned conjugate gradient algorithm, function of several variables using first derivatives (comprehensive)
- E04DJF Read optional parameter values for E04DGF/E04DGA from external file
- E04DKF Supply optional parameter values to E04DGF/E04DGA
- E04FCF Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm using function values only (comprehensive)
- E04FYF Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm using function values only (easy-to-use)
- E04GBF Unconstrained minimum of a sum of squares, combined Gauss–Newton and quasi-Newton algorithm using first derivatives (comprehensive)
- E04GDF Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm using first derivatives (comprehensive)
- E04GYF Unconstrained minimum of a sum of squares, combined Gauss–Newton and quasi-Newton algorithm, using first derivatives (easy-to-use)
- E04GZF Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm using first derivatives (easy-to-use)
- E04HCF Check user’s routine for calculating first derivatives of function
- E04HDF Check user’s routine for calculating second derivatives of function
- E04HEF Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm, using second derivatives (comprehensive)
- E04HYF Unconstrained minimum of a sum of squares, combined Gauss–Newton and modified Newton algorithm, using second derivatives (easy-to-use)
- E04JYF Minimum, function of several variables, quasi-Newton algorithm, simple bounds, using function values only (easy-to-use)
- E04KDF Minimum, function of several variables, modified Newton algorithm, simple bounds, using first derivatives (comprehensive)
- E04KYF Minimum, function of several variables, quasi-Newton algorithm, simple bounds, using first derivatives (easy-to-use)
- E04KZF Minimum, function of several variables, modified Newton algorithm, simple bounds, using first derivatives (easy-to-use)
- E04LBF Minimum, function of several variables, modified Newton algorithm, simple bounds, using first and second derivatives (comprehensive)
- E04LYF Minimum, function of several variables, modified Newton algorithm, simple bounds, using first and second derivatives (easy-to-use)
- E04MFF LP problem (dense)
- E04MGF Read optional parameter values for E04MFF/E04MFA from external file
- E04MHF Supply optional parameter values to E04MFF/E04MFA
- E04MZF Converts MPSX data file defining LP or QP problem to format required by E04NKF/E04NKA
- E04NCF Convex QP problem or linearly-constrained linear least-squares problem (dense)
- E04NDF Read optional parameter values for E04NCF/E04NCA from external file
- E04NEF Supply optional parameter values to E04NCF/E04NCA
- E04NFF QP problem (dense)
- E04NGF Read optional parameter values for E04NFF/E04NFA from external file
- E04NHF Supply optional parameter values to E04NFF/E04NFA
- E04NKF LP or QP problem (sparse)
- E04NLF Read optional parameter values for E04NKF/E04NKA from external file
- E04NMF Supply optional parameter values to E04NKF/E04NKA
- E04UCF Minimum, function of several variables, sequential QP method, nonlinear constraints, using function values and optionally first derivatives (forward communication, comprehensive)
- E04UDF Read optional parameter values for E04UCF/E04UCA or E04UFF/E04UFA from external file
- E04UEF Supply optional parameter values to E04UCF/E04UCA or E04UFF/E04UFA
- E04UFF Minimum, function of several variables, sequential QP method, nonlinear constraints, using function values and optionally first derivatives (reverse communication, comprehensive)

|        |  |
|--------|--|
| E04UGF | NLP problem (sparse)   |
| E04UHF | Read optional parameter values for E04UGF/E04UGA from external file  |
| E04UJF | Supply optional parameter values to E04UGF/E04UGA  |
| E04UNF | Minimum of a sum of squares, nonlinear constraints, sequential QP method, using function values and optionally first derivatives (comprehensive) |
| E04UQF | Read optional parameter values for E04USF/E04USA from external file  |
| E04URF | Supply optional parameter values to E04USF/E04USA  |
| E04USF | Minimum of a sum of squares, nonlinear constraints, sequential QP method, using function values and optionally first derivatives (comprehensive) |
| E04WBF | Initialization routine for E04DGA, E04MFA, E04NCA, E04NFA, E04NKA, E04UCA, E04UFA, E04UGA and E04USA   |
| E04XAF | Estimate (using numerical differentiation) gradient and/or Hessian of a function   |
| E04YAF | Check user's routine for calculating Jacobian of first derivatives   |
| E04YBF | Check user's routine for calculating Hessian of a sum of squares   |
| E04YCF | Covariance matrix for nonlinear least-squares problem (unconstrained)  |
| E04ZCF | Check user's routines for calculating first derivatives of function and constraints  |

## F01 – Matrix Factorizations

|        |  |
|--------|--|
| F01ABF | Inverse of real symmetric positive-definite matrix using iterative refinement              |
| F01ADF | Inverse of real symmetric positive-definite matrix   |
| F01BLF | Pseudo-inverse and rank of real $m$ by $n$ matrix ( $m \geq n$ )                           |
| F01BRF | $LU$ factorization of real sparse matrix   |
| F01BSF | $LU$ factorization of real sparse matrix with known sparsity pattern                       |
| F01BUF | $ULDL^T U^T$ factorization of real symmetric positive-definite band matrix                 |
| F01BVF | Reduction to standard form, generalized real symmetric-definite banded eigenproblem        |
| F01CKF | Matrix multiplication  |
| F01CRF | Matrix transposition   |
| F01CTF | Sum or difference of two real matrices, optional scaling and transposition                 |
| F01CWF | Sum or difference of two complex matrices, optional scaling and transposition              |
| F01LEF | $LU$ factorization of real tridiagonal matrix  |
| F01LHF | $LU$ factorization of real almost block diagonal matrix                                    |
| F01MCF | $LDL^T$ factorization of real symmetric positive-definite variable-bandwidth matrix        |
| F01QGF | $RQ$ factorization of real $m$ by $n$ upper trapezoidal matrix ( $m \leq n$ )              |
| F01QJF | $RQ$ factorization of real $m$ by $n$ matrix ( $m \leq n$ )                                |
| F01QKF | Operations with orthogonal matrices, form rows of $Q$ , after $RQ$ factorization by F01QJF |
| F01RGF | $RQ$ factorization of complex $m$ by $n$ upper trapezoidal matrix ( $m \leq n$ )           |
| F01RJF | $RQ$ factorization of complex $m$ by $n$ matrix ( $m \leq n$ )                             |
| F01RKF | Operations with unitary matrices, form rows of $Q$ , after $RQ$ factorization by F01RJF    |
| F01ZAF | Convert real matrix between packed triangular and square storage schemes                   |
| F01ZBF | Convert complex matrix between packed triangular and square storage schemes                |
| F01ZCF | Convert real matrix between packed banded and rectangular storage schemes                  |
| F01ZDF | Convert complex matrix between packed banded and rectangular storage schemes               |

## F02 – Eigenvalues and Eigenvectors

|        |  |
|--------|--|
| F02BJF | All eigenvalues and optionally eigenvectors of generalized eigenproblem by $QZ$ algorithm, real matrices (Black Box) |
| F02EAF | All eigenvalues and Schur factorization of real general matrix (Black Box)   |
| F02EBF | All eigenvalues and eigenvectors of real general matrix (Black Box)  |
| F02ECF | Selected eigenvalues and eigenvectors of real nonsymmetric matrix (Black Box)  |
| F02FAF | All eigenvalues and eigenvectors of real symmetric matrix (Black Box)  |
| F02FCF | Selected eigenvalues and eigenvectors of real symmetric matrix (Black Box)   |
| F02FDF | All eigenvalues and eigenvectors of real symmetric-definite generalized problem (Black Box)                          |
| F02FHF | All eigenvalues of generalized banded real symmetric-definite eigenproblem (Black Box)                               |
| F02FJF | Selected eigenvalues and eigenvectors of sparse symmetric eigenproblem (Black Box)                                   |
| F02GAF | All eigenvalues and Schur factorization of complex general matrix (Black Box)  |
| F02GBF | All eigenvalues and eigenvectors of complex general matrix (Black Box)   |



- F02GCF Selected eigenvalues and eigenvectors of complex nonsymmetric matrix (Black Box)  
 F02GJF All eigenvalues and optionally eigenvectors of generalized complex eigenproblem by  $QZ$  algorithm (Black Box)  
 F02HAF All eigenvalues and eigenvectors of complex Hermitian matrix (Black Box)  
 F02HCF Selected eigenvalues and eigenvectors of complex Hermitian matrix (Black Box)  
 F02HDF All eigenvalues and eigenvectors of complex Hermitian-definite generalized problem (Black Box)  
 F02SDF Eigenvector of generalized real banded eigenproblem by inverse iteration  
 F02WDF  $QR$  factorization, possibly followed by SVD  
 F02WEF SVD of real matrix (Black Box)  
 F02WUF SVD of real upper triangular matrix (Black Box)  
 F02XEF SVD of complex matrix (Black Box)  
 F02XUF SVD of complex upper triangular matrix (Black Box)

### F03 – Determinants

- F03AAF Determinant of real matrix (Black Box)  
 F03ABF Determinant of real symmetric positive-definite matrix (Black Box)  
 F03ACF Determinant of real symmetric positive-definite band matrix (Black Box)  
 F03ADF Determinant of complex matrix (Black Box)  
 F03AEF  $LL^T$  factorization and determinant of real symmetric positive-definite matrix  
 F03AFF  $LU$  factorization and determinant of real matrix

### F04 – Simultaneous Linear Equations

- F04AAF Solution of real simultaneous linear equations with multiple right-hand sides (Black Box)  
 F04ABF Solution of real symmetric positive-definite simultaneous linear equations with multiple right-hand sides using iterative refinement (Black Box)  
 F04ACF Solution of real symmetric positive-definite banded simultaneous linear equations with multiple right-hand sides (Black Box)  
 F04ADF Solution of complex simultaneous linear equations with multiple right-hand sides (Black Box)  
 F04AEF Solution of real simultaneous linear equations with multiple right-hand sides using iterative refinement (Black Box)  
 F04AFF Solution of real symmetric positive-definite simultaneous linear equations using iterative refinement (coefficient matrix already factorized by F03AEF)  
 F04AGF Solution of real symmetric positive-definite simultaneous linear equations (coefficient matrix already factorized by F03AEF)  
 F04AHF Solution of real simultaneous linear equations using iterative refinement (coefficient matrix already factorized by F03AFF)  
 F04AJF Solution of real simultaneous linear equations (coefficient matrix already factorized by F03AFF)  
 F04AMF Least-squares solution of  $m$  real equations in  $n$  unknowns, rank =  $n$ ,  $m \geq n$  using iterative refinement (Black Box)  
 F04ARF Solution of real simultaneous linear equations, one right-hand side (Black Box)  
 F04ASF Solution of real symmetric positive-definite simultaneous linear equations, one right-hand side using iterative refinement (Black Box)  
 F04ATF Solution of real simultaneous linear equations, one right-hand side using iterative refinement (Black Box)  
 F04AXF Solution of real sparse simultaneous linear equations (coefficient matrix already factorized)  
 F04EAF Solution of real tridiagonal simultaneous linear equations, one right-hand side (Black Box)  
 F04FAF Solution of real symmetric positive-definite tridiagonal simultaneous linear equations, one right-hand side (Black Box)  
 F04FEF Solution of the Yule–Walker equations for real symmetric positive-definite Toeplitz matrix, one right-hand side  
 F04FFF Solution of real symmetric positive-definite Toeplitz system, one right-hand side  
 F04JAF Minimal least-squares solution of  $m$  real equations in  $n$  unknowns, rank  $\leq n$ ,  $m \geq n$   
 F04JDF Minimal least-squares solution of  $m$  real equations in  $n$  unknowns, rank  $\leq n$ ,  $m \geq n$   
 F04JGF Least-squares (if rank =  $n$ ) or minimal least-squares (if rank  $< n$ ) solution of  $m$  real equations in  $n$  unknowns, rank  $\leq n$ ,  $m \geq n$   
 F04JLF Real general Gauss–Markov linear model (including weighted least-squares)

|        |   |
|--------|---|
| F04JMF | Equality-constrained real linear least-squares problem  |
| F04KLF | Complex general Gauss–Markov linear model (including weighted least-squares)  |
| F04KMF | Equality-constrained complex linear least-squares problem   |
| F04LEF | Solution of real tridiagonal simultaneous linear equations (coefficient matrix already factorized by F01LEF)                                    |
| F04LHF | Solution of real almost block diagonal simultaneous linear equations (coefficient matrix already factorized by F01LHF)                          |
| F04MCF | Solution of real symmetric positive-definite variable-bandwidth simultaneous linear equations (coefficient matrix already factorized by F01MCF) |
| F04MEF | Update solution of the Yule–Walker equations for real symmetric positive-definite Toeplitz matrix   |
| F04MFF | Update solution of real symmetric positive-definite Toeplitz system   |
| F04QAF | Sparse linear least-squares problem, $m$ real equations in $n$ unknowns   |
| F04YAF | Covariance matrix for linear least-squares problems, $m$ real equations in $n$ unknowns   |
| F04YCF | Norm estimation (for use in condition estimation), real matrix  |
| F04ZCF | Norm estimation (for use in condition estimation), complex matrix   |

## F05 – Orthogonalisation

|        |  |
|--------|--|
| F05AAF | Gram–Schmidt orthogonalisation of $n$ vectors of order $m$ |
|--------|--|

## F06 – Linear Algebra Support Routines

|        |   |
|--------|---|
| F06AAF | Generate real plane rotation                                    |
| F06BAF | Generate real plane rotation, storing tangent                   |
| F06BCF | Recover cosine and sine from given real tangent                 |
| F06BEF | Generate real Jacobi plane rotation                             |
| F06BHF | Apply real similarity rotation to 2 by 2 symmetric matrix       |
| F06BLF | Compute quotient of two real scalars, with overflow flag        |
| F06BMF | Compute Euclidean norm from scaled form                         |
| F06BNF | Compute square root of $(a^2 + b^2)$ , real $a$ and $b$         |
| F06BPF | Compute eigenvalue of 2 by 2 real symmetric matrix              |
| F06CAF | Generate complex plane rotation, storing tangent, real cosine   |
| F06CBF | Generate complex plane rotation, storing tangent, real sine     |
| F06CCF | Recover cosine and sine from given complex tangent, real cosine |
| F06CDF | Recover cosine and sine from given complex tangent, real sine   |
| F06CHF | Apply complex similarity rotation to 2 by 2 Hermitian matrix    |
| F06CLF | Compute quotient of two complex scalars, with overflow flag     |
| F06DBF | Broadcast scalar into integer vector                            |
| F06DFF | Copy integer vector   |
| F06EAF | Dot product of two real vectors                                 |
| F06ECF | Add scalar times real vector to real vector                     |
| F06EDF | Multiply real vector by scalar                                  |
| F06EFF | Copy real vector  |
| F06EGF | Swap two real vectors   |
| F06EJF | Compute Euclidean norm of real vector                           |
| F06EKF | Sum absolute values of real vector elements                     |
| F06EPF | Apply real plane rotation                                       |
| F06ERF | Dot product of two real sparse vectors                          |
| F06ETF | Add scalar times real sparse vector to real sparse vector       |
| F06EUF | Gather real sparse vector                                       |
| F06EVF | Gather and set to zero real sparse vector                       |
| F06EWF | Scatter real sparse vector                                      |
| F06EXF | Apply plane rotation to two real sparse vectors                 |
| F06FAF | Compute cosine of angle between two real vectors                |
| F06FBF | Broadcast scalar into real vector                               |
| F06FCF | Multiply real vector by diagonal matrix                         |
| F06FDF | Multiply real vector by scalar, preserving input vector         |
| F06FGF | Negate real vector  |

|        |  |
|--------|--|
| F06FJF | Update Euclidean norm of real vector in scaled form  |
| F06FKF | Compute weighted Euclidean norm of real vector   |
| F06FLF | Elements of real vector with largest and smallest absolute value                               |
| F06FPF | Apply real symmetric plane rotation to two vectors   |
| F06FQF | Generate sequence of real plane rotations  |
| F06FRF | Generate real elementary reflection, NAG style   |
| F06FSF | Generate real elementary reflection, LINPACK style   |
| F06FTF | Apply real elementary reflection, NAG style  |
| F06FUF | Apply real elementary reflection, LINPACK style  |
| F06GAF | Dot product of two complex vectors, unconjugated   |
| F06GBF | Dot product of two complex vectors, conjugated   |
| F06GCF | Add scalar times complex vector to complex vector  |
| F06GDF | Multiply complex vector by complex scalar  |
| F06GFF | Copy complex vector  |
| F06GGF | Swap two complex vectors   |
| F06GRF | Dot product of two complex sparse vector, unconjugated   |
| F06GSF | Dot product of two complex sparse vector, conjugated   |
| F06GTF | Add scalar times complex sparse vector to complex sparse vector                                |
| F06GUF | Gather complex sparse vector   |
| F06GVF | Gather and set to zero complex sparse vector   |
| F06GWF | Scatter complex sparse vector  |
| F06HBF | Broadcast scalar into complex vector   |
| F06HCF | Multiply complex vector by complex diagonal matrix   |
| F06HDF | Multiply complex vector by complex scalar, preserving input vector                             |
| F06HGF | Negate complex vector  |
| F06HPF | Apply complex plane rotation   |
| F06HQF | Generate sequence of complex plane rotations   |
| F06HRF | Generate complex elementary reflection   |
| F06HTF | Apply complex elementary reflection  |
| F06JDF | Multiply complex vector by real scalar   |
| F06JJF | Compute Euclidean norm of complex vector   |
| F06JKF | Sum absolute values of complex vector elements   |
| F06JLF | Index, real vector element with largest absolute value   |
| F06JMF | Index, complex vector element with largest absolute value                                      |
| F06KCF | Multiply complex vector by real diagonal matrix  |
| F06KDF | Multiply complex vector by real scalar, preserving input vector                                |
| F06KFF | Copy real vector to complex vector   |
| F06KJF | Update Euclidean norm of complex vector in scaled form   |
| F06KLF | Last non-negligible element of real vector   |
| F06KPF | Apply real plane rotation to two complex vectors   |
| F06PAF | Matrix-vector product, real rectangular matrix   |
| F06PBF | Matrix-vector product, real rectangular band matrix  |
| F06PCF | Matrix-vector product, real symmetric matrix   |
| F06PDF | Matrix-vector product, real symmetric band matrix  |
| F06PEF | Matrix-vector product, real symmetric packed matrix  |
| F06PFF | Matrix-vector product, real triangular matrix  |
| F06PGF | Matrix-vector product, real triangular band matrix   |
| F06PHF | Matrix-vector product, real triangular packed matrix   |
| F06PJF | System of equations, real triangular matrix  |
| F06PKF | System of equations, real triangular band matrix   |
| F06PLF | System of equations, real triangular packed matrix   |
| F06PMF | Rank-1 update, real rectangular matrix   |
| F06PPF | Rank-1 update, real symmetric matrix   |
| F06PQF | Rank-1 update, real symmetric packed matrix  |
| F06PRF | Rank-2 update, real symmetric matrix   |
| F06PSF | Rank-2 update, real symmetric packed matrix  |
| F06QFF | Matrix copy, real rectangular or trapezoidal matrix  |
| F06QHF | Matrix initialisation, real rectangular matrix   |
| F06QJF | Permute rows or columns, real rectangular matrix, permutations represented by an integer array |

|        |  |
|--------|--|
| F06QKF | Permute rows or columns, real rectangular matrix, permutations represented by a real array                                 |
| F06QMF | Orthogonal similarity transformation of real symmetric matrix as a sequence of plane rotations                             |
| F06QPF | $QR$ factorization by sequence of plane rotations, rank-1 update of real upper triangular matrix                           |
| F06QQF | $QR$ factorization by sequence of plane rotations, real upper triangular matrix augmented by a full row                    |
| F06QRF | $QR$ or $RQ$ factorization by sequence of plane rotations, real upper Hessenberg matrix                                    |
| F06QSF | $QR$ or $RQ$ factorization by sequence of plane rotations, real upper spiked matrix  |
| F06QTF | $QR$ factorization of $UZ$ or $RQ$ factorization of $ZU$ , $U$ real upper triangular, $Z$ a sequence of plane rotations    |
| F06QVF | Compute upper Hessenberg matrix by sequence of plane rotations, real upper triangular matrix                               |
| F06QWF | Compute upper spiked matrix by sequence of plane rotations, real upper triangular matrix                                   |
| F06QXF | Apply sequence of plane rotations, real rectangular matrix   |
| F06RAF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real general matrix                                      |
| F06RBF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real band matrix   |
| F06RCF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real symmetric matrix                                    |
| F06RDF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real symmetric matrix, packed storage                    |
| F06REF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real symmetric band matrix                               |
| F06RJF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real trapezoidal/triangular matrix                       |
| F06RKF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real triangular matrix, packed storage                   |
| F06RLF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real triangular band matrix                              |
| F06RMF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, real Hessenberg matrix                                   |
| F06SAF | Matrix-vector product, complex rectangular matrix  |
| F06SBF | Matrix-vector product, complex rectangular band matrix   |
| F06SCF | Matrix-vector product, complex Hermitian matrix  |
| F06SDF | Matrix-vector product, complex Hermitian band matrix   |
| F06SEF | Matrix-vector product, complex Hermitian packed matrix   |
| F06SFF | Matrix-vector product, complex triangular matrix   |
| F06SGF | Matrix-vector product, complex triangular band matrix  |
| F06SHF | Matrix-vector product, complex triangular packed matrix  |
| F06SJF | System of equations, complex triangular matrix   |
| F06SKF | System of equations, complex triangular band matrix  |
| F06SLF | System of equations, complex triangular packed matrix  |
| F06SMF | Rank-1 update, complex rectangular matrix, unconjugated vector   |
| F06SNF | Rank-1 update, complex rectangular matrix, conjugated vector   |
| F06SPF | Rank-1 update, complex Hermitian matrix  |
| F06SQF | Rank-1 update, complex Hermitian packed matrix   |
| F06SRF | Rank-2 update, complex Hermitian matrix  |
| F06SSF | Rank-2 update, complex Hermitian packed matrix   |
| F06TFF | Matrix copy, complex rectangular or trapezoidal matrix   |
| F06THF | Matrix initialisation, complex rectangular matrix  |
| F06TMF | Unitary similarity transformation of Hermitian matrix as a sequence of plane rotations                                     |
| F06TPF | $QR$ factorization by sequence of plane rotations, rank-1 update of complex upper triangular matrix                        |
| F06TQF | $QR \times k$ factorization by sequence of plane rotations, complex upper triangular matrix augmented by a full row        |
| F06TRF | $QR$ or $RQ$ factorization by sequence of plane rotations, complex upper Hessenberg matrix                                 |
| F06TSF | $QR$ or $RQ$ factorization by sequence of plane rotations, complex upper spiked matrix                                     |
| F06TTF | $QR$ factorization of $UZ$ or $RQ$ factorization of $ZU$ , $U$ complex upper triangular, $Z$ a sequence of plane rotations |
| F06TVF | Compute upper Hessenberg matrix by sequence of plane rotations, complex upper triangular matrix                            |
| F06TWF | Compute upper spiked matrix by sequence of plane rotations, complex upper triangular matrix                                |
| F06TXF | Apply sequence of plane rotations, complex rectangular matrix, real cosine and complex sine                                |
| F06TYF | Apply sequence of plane rotations, complex rectangular matrix, complex cosine and real sine                                |
| F06UAF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex general matrix                                   |
| F06UBF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex band matrix                                      |
| F06UCF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex Hermitian matrix                                 |

|        |   |
|--------|---|
| F06UDF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex Hermitian matrix, packed storage  |
| F06UEF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex Hermitian band matrix             |
| F06UFF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex symmetric matrix                  |
| F06UGF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex symmetric matrix, packed storage  |
| F06UHF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex symmetric band matrix             |
| F06UJF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex trapezoidal/triangular matrix     |
| F06UKF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex triangular matrix, packed storage |
| F06ULF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex triangular band matrix            |
| F06UMF | 1-norm, $\infty$ -norm, Frobenius norm, largest absolute element, complex Hessenberg matrix                 |
| F06VJF | Permute rows or columns, complex rectangular matrix, permutations represented by an integer array           |
| F06VKF | Permute rows or columns, complex rectangular matrix, permutations represented by a real array               |
| F06VXF | Apply sequence of plane rotations, complex rectangular matrix, real cosine and sine                         |
| F06YAF | Matrix-matrix product, two real rectangular matrices  |
| F06YCF | Matrix-matrix product, one real symmetric matrix, one real rectangular matrix                               |
| F06YFF | Matrix-matrix product, one real triangular matrix, one real rectangular matrix                              |
| F06YJF | Solves system of equations with multiple right-hand sides, real triangular coefficient matrix               |
| F06YPF | Rank- $k$ update of real symmetric matrix   |
| F06YRF | Rank- $2k$ update of real symmetric matrix  |
| F06ZAF | Matrix-matrix product, two complex rectangular matrices   |
| F06ZCF | Matrix-matrix product, one complex Hermitian matrix, one complex rectangular matrix                         |
| F06ZFF | Matrix-matrix product, one complex triangular matrix, one complex rectangular matrix                        |
| F06ZJF | Solves system of equations with multiple right-hand sides, complex triangular coefficient matrix            |
| F06ZPF | Rank- $k$ update of complex Hermitian matrix  |
| F06ZRF | Rank- $2k$ update of complex Hermitian matrix   |
| F06ZTF | Matrix-matrix product, one complex symmetric matrix, one complex rectangular matrix                         |
| F06ZUF | Rank- $k$ update of complex symmetric matrix  |
| F06ZWF | Rank- $2k$ update of complex symmetric matrix   |

## F07 – Linear Equations (LAPACK)

A list of the LAPACK equivalent names is included in the F07 Chapter Introduction.

|        |  |
|--------|--|
| F07ADF | $LU$ factorization of real $m$ by $n$ matrix   |
| F07AEF | Solution of real system of linear equations, multiple right-hand sides, matrix already factorized by F07ADF (SGETRF/DGETRF)      |
| F07AGF | Estimate condition number of real matrix, matrix already factorized by F07ADF (SGETRF/DGETRF)                                    |
| F07AHF | Refined solution with error bounds of real system of linear equations, multiple right-hand sides                                 |
| F07AJF | Inverse of real matrix, matrix already factorized by F07ADF (SGETRF/DGETRF)  |
| F07ARF | $LU$ factorization of complex $m$ by $n$ matrix  |
| F07ASF | Solution of complex system of linear equations, multiple right-hand sides, matrix already factorized by F07ARF (CGETRF/ZGETRF)   |
| F07AUF | Estimate condition number of complex matrix, matrix already factorized by F07ARF (CGETRF/ZGETRF)                                 |
| F07AVF | Refined solution with error bounds of complex system of linear equations, multiple right-hand sides                              |
| F07AWF | Inverse of complex matrix, matrix already factorized by F07ARF (CGETRF/ZGETRF)   |
| F07BDF | $LU$ factorization of real $m$ by $n$ band matrix  |
| F07BEF | Solution of real band system of linear equations, multiple right-hand sides, matrix already factorized by F07BDF (SGBTRF/DGBTRF) |
| F07BGF | Estimate condition number of real band matrix, matrix already factorized by F07BDF (SGBTRF/DGBTRF)                               |
| F07BHF | Refined solution with error bounds of real band system of linear equations, multiple right-hand sides                            |

|        |  |
|--------|--|
| F07BRF | <i>LU</i> factorization of complex $m$ by $n$ band matrix  |
| F07BSF | Solution of complex band system of linear equations, multiple right-hand sides, matrix already factorized by F07BRF (CGBTRF/ZGBTRF)  |
| F07BUF | Estimate condition number of complex band matrix, matrix already factorized by F07BRF (CGBTRF/ZGBTRF)  |
| F07BVF | Refined solution with error bounds of complex band system of linear equations, multiple right-hand sides   |
| F07FDF | Cholesky factorization of real symmetric positive-definite matrix  |
| F07FEF | Solution of real symmetric positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07FDF (SPOTRF/DPOTRF)                    |
| F07FGF | Estimate condition number of real symmetric positive-definite matrix, matrix already factorized by F07FDF (SPOTRF/DPOTRF)  |
| F07FHF | Refined solution with error bounds of real symmetric positive-definite system of linear equations, multiple right-hand sides   |
| F07FJF | Inverse of real symmetric positive-definite matrix, matrix already factorized by F07FDF (SPOTRF/DPOTRF)  |
| F07FRF | Cholesky factorization of complex Hermitian positive-definite matrix   |
| F07FSF | Solution of complex Hermitian positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07FRF (CPOTRF/ZPOTRF)                 |
| F07FUF | Estimate condition number of complex Hermitian positive-definite matrix, matrix already factorized by F07FRF (CPOTRF/ZPOTRF)   |
| F07FVF | Refined solution with error bounds of complex Hermitian positive-definite system of linear equations, multiple right-hand sides  |
| F07FWF | Inverse of complex Hermitian positive-definite matrix, matrix already factorized by F07FRF (CPOTRF/ZPOTRF)   |
| F07GDF | Cholesky factorization of real symmetric positive-definite matrix, packed storage  |
| F07GEF | Solution of real symmetric positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07GDF (SPPTRF/DPPTRF), packed storage    |
| F07GGF | Estimate condition number of real symmetric positive-definite matrix, matrix already factorized by F07GDF (SPPTRF/DPPTRF), packed storage                                  |
| F07GHF | Refined solution with error bounds of real symmetric positive-definite system of linear equations, multiple right-hand sides, packed storage                               |
| F07GJF | Inverse of real symmetric positive-definite matrix, matrix already factorized by F07GDF (SPPTRF/DPPTRF), packed storage  |
| F07GRF | Cholesky factorization of complex Hermitian positive-definite matrix, packed storage   |
| F07GSF | Solution of complex Hermitian positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07GRF (CPPTRF/ZPPTRF), packed storage |
| F07GUF | Estimate condition number of complex Hermitian positive-definite matrix, matrix already factorized by F07GRF (CPPTRF/ZPPTRF), packed storage                               |
| F07GVF | Refined solution with error bounds of complex Hermitian positive-definite system of linear equations, multiple right-hand sides, packed storage                            |
| F07GWF | Inverse of complex Hermitian positive-definite matrix, matrix already factorized by F07GRF (CPPTRF/ZPPTRF), packed storage   |
| F07HDF | Cholesky factorization of real symmetric positive-definite band matrix   |
| F07HEF | Solution of real symmetric positive-definite band system of linear equations, multiple right-hand sides, matrix already factorized by F07HDF (SPBTRF/DPBTRF)               |
| F07HGF | Estimate condition number of real symmetric positive-definite band matrix, matrix already factorized by F07HDF (SPBTRF/DPBTRF)   |
| F07HHF | Refined solution with error bounds of real symmetric positive-definite band system of linear equations, multiple right-hand sides  |
| F07HRF | Cholesky factorization of complex Hermitian positive-definite band matrix  |
| F07HSF | Solution of complex Hermitian positive-definite band system of linear equations, multiple right-hand sides, matrix already factorized by F07HRF (CPBTRF/ZPBTRF)            |
| F07HUF | Estimate condition number of complex Hermitian positive-definite band matrix, matrix already factorized by F07HRF (CPBTRF/ZPBTRF)  |
| F07HVF | Refined solution with error bounds of complex Hermitian positive-definite band system of linear equations, multiple right-hand sides                                       |
| F07MDF | Bunch–Kaufman factorization of real symmetric indefinite matrix  |

|        |   |
|--------|---|
| F07MEF | Solution of real symmetric indefinite system of linear equations, multiple right-hand sides, matrix already factorized by F07MDF (SSYTRF/DSYTRF)                    |
| F07MGF | Estimate condition number of real symmetric indefinite matrix, matrix already factorized by F07MDF (SSYTRF/DSYTRF)  |
| F07MHF | Refined solution with error bounds of real symmetric indefinite system of linear equations, multiple right-hand sides   |
| F07MJF | Inverse of real symmetric indefinite matrix, matrix already factorized by F07MDF (SSYTRF/DSYTRF)  |
| F07MRF | Bunch–Kaufman factorization of complex Hermitian indefinite matrix  |
| F07MSF | Solution of complex Hermitian indefinite system of linear equations, multiple right-hand sides, matrix already factorized by F07MRF (CHETRF/ZHETRF)                 |
| F07MUF | Estimate condition number of complex Hermitian indefinite matrix, matrix already factorized by F07MRF (CHETRF/ZHETRF)   |
| F07MVF | Refined solution with error bounds of complex Hermitian indefinite system of linear equations, multiple right-hand sides  |
| F07MWF | Inverse of complex Hermitian indefinite matrix, matrix already factorized by F07MRF (CHETRF/ZHETRF)   |
| F07NRF | Bunch–Kaufman factorization of complex symmetric matrix   |
| F07NSF | Solution of complex symmetric system of linear equations, multiple right-hand sides, matrix already factorized by F07NRF (CSYTRF/ZSYTRF)                            |
| F07NUF | Estimate condition number of complex symmetric matrix, matrix already factorized by F07NRF (CSYTRF/ZSYTRF)  |
| F07NVF | Refined solution with error bounds of complex symmetric system of linear equations, multiple right-hand sides   |
| F07NWF | Inverse of complex symmetric matrix, matrix already factorized by F07NRF (CSYTRF/ZSYTRF)  |
| F07PDF | Bunch–Kaufman factorization of real symmetric indefinite matrix, packed storage   |
| F07PEF | Solution of real symmetric indefinite system of linear equations, multiple right-hand sides, matrix already factorized by F07PDF (SSPTRF/DSPTRF), packed storage    |
| F07PGF | Estimate condition number of real symmetric indefinite matrix, matrix already factorized by F07PDF (SSPTRF/DSPTRF), packed storage                                  |
| F07PHF | Refined solution with error bounds of real symmetric indefinite system of linear equations, multiple right-hand sides, packed storage                               |
| F07PJF | Inverse of real symmetric indefinite matrix, matrix already factorized by F07PDF (SSPTRF/DSPTRF), packed storage  |
| F07PRF | Bunch–Kaufman factorization of complex Hermitian indefinite matrix, packed storage  |
| F07PSF | Solution of complex Hermitian indefinite system of linear equations, multiple right-hand sides, matrix already factorized by F07PRF (CHPTRF/ZHPTRF), packed storage |
| F07PUF | Estimate condition number of complex Hermitian indefinite matrix, matrix already factorized by F07PRF (CHPTRF/ZHPTRF), packed storage                               |
| F07PVF | Refined solution with error bounds of complex Hermitian indefinite system of linear equations, multiple right-hand sides, packed storage                            |
| F07PWF | Inverse of complex Hermitian indefinite matrix, matrix already factorized by F07PRF (CHPTRF/ZHPTRF), packed storage   |
| F07QRF | Bunch–Kaufman factorization of complex symmetric matrix, packed storage   |
| F07QSF | Solution of complex symmetric system of linear equations, multiple right-hand sides, matrix already factorized by F07QRF (CSPTRF/ZSPTRF), packed storage            |
| F07QUF | Estimate condition number of complex symmetric matrix, matrix already factorized by F07QRF (CSPTRF/ZSPTRF), packed storage  |
| F07QVF | Refined solution with error bounds of complex symmetric system of linear equations, multiple right-hand sides, packed storage                                       |
| F07QWF | Inverse of complex symmetric matrix, matrix already factorized by F07QRF (CSPTRF/ZSPTRF), packed storage  |
| F07TEF | Solution of real triangular system of linear equations, multiple right-hand sides   |
| F07TGF | Estimate condition number of real triangular matrix   |
| F07THF | Error bounds for solution of real triangular system of linear equations, multiple right-hand sides  |
| F07TJF | Inverse of real triangular matrix   |
| F07TSF | Solution of complex triangular system of linear equations, multiple right-hand sides  |
| F07TUF | Estimate condition number of complex triangular matrix  |

|        |   |
|--------|---|
| F07TVF | Error bounds for solution of complex triangular system of linear equations, multiple right-hand sides                 |
| F07TWF | Inverse of complex triangular matrix  |
| F07UEF | Solution of real triangular system of linear equations, multiple right-hand sides, packed storage                     |
| F07UGF | Estimate condition number of real triangular matrix, packed storage   |
| F07UHF | Error bounds for solution of real triangular system of linear equations, multiple right-hand sides, packed storage    |
| F07UJF | Inverse of real triangular matrix, packed storage   |
| F07USF | Solution of complex triangular system of linear equations, multiple right-hand sides, packed storage                  |
| F07UUF | Estimate condition number of complex triangular matrix, packed storage  |
| F07UVF | Error bounds for solution of complex triangular system of linear equations, multiple right-hand sides, packed storage |
| F07UWF | Inverse of complex triangular matrix, packed storage  |
| F07VEF | Solution of real band triangular system of linear equations, multiple right-hand sides                                |
| F07VGF | Estimate condition number of real band triangular matrix  |
| F07VHF | Error bounds for solution of real band triangular system of linear equations, multiple right-hand sides               |
| F07VSF | Solution of complex band triangular system of linear equations, multiple right-hand sides                             |
| F07VUF | Estimate condition number of complex band triangular matrix   |
| F07VVF | Error bounds for solution of complex band triangular system of linear equations, multiple right-hand sides            |

## F08 – Least-squares and Eigenvalue Problems (LAPACK)

A list of the LAPACK equivalent names is included in the F08 Chapter Introduction.

|        |   |
|--------|---|
| F08AEF | $QR$ factorization of real general rectangular matrix   |
| F08AFF | Form all or part of orthogonal $Q$ from $QR$ factorization determined by F08AEF (SGEQRF/DGEQRF) or F08BEF (SGEQPF/DGEQPF) |
| F08AGF | Apply orthogonal transformation determined by F08AEF (SGEQRF/DGEQRF) or F08BEF (SGEQPF/DGEQPF)                            |
| F08AHF | $LQ$ factorization of real general rectangular matrix   |
| F08AJF | Form all or part of orthogonal $Q$ from $LQ$ factorization determined by F08AHF (SGELQF/DGELQF)                           |
| F08AKF | Apply orthogonal transformation determined by F08AHF (SGELQF/DGELQF)  |
| F08ASF | $QR$ factorization of complex general rectangular matrix  |
| F08ATF | Form all or part of unitary $Q$ from $QR$ factorization determined by F08ASF (CGEQRF/ZGEQRF) or F08BSF (CGEQPF/ZGEQPF)    |
| F08AUF | Apply unitary transformation determined by F08ASF (CGEQRF/ZGEQRF) or F08BSF (CGEQPF/ZGEQPF)                               |
| F08AVF | $LQ$ factorization of complex general rectangular matrix  |
| F08AWF | Form all or part of unitary $Q$ from $LQ$ factorization determined by F08AVF (CGELQF/ZGELQF)                              |
| F08AXF | Apply unitary transformation determined by F08AVF (CGELQF/ZGELQF)   |
| F08BEF | $QR$ factorization of real general rectangular matrix with column pivoting  |
| F08BSF | $QR$ factorization of complex general rectangular matrix with column pivoting   |
| F08FCF | All eigenvalues and optionally all eigenvectors of real symmetric matrix, using divide and conquer                        |
| F08FEF | Orthogonal reduction of real symmetric matrix to symmetric tridiagonal form   |
| F08FFF | Generate orthogonal transformation matrix from reduction to tridiagonal form determined by F08FEF (SSYTRD/DSYTRD)         |
| F08FGF | Apply orthogonal transformation determined by F08FEF (SSYTRD/DSYTRD)  |
| F08FQF | All eigenvalues and optionally all eigenvectors of complex Hermitian matrix, using divide and conquer                     |
| F08FSF | Unitary reduction of complex Hermitian matrix to real symmetric tridiagonal form  |
| F08FTF | Generate unitary transformation matrix from reduction to tridiagonal form determined by F08FSF (CHETRD/ZHETRD)            |
| F08FUF | Apply unitary transformation matrix determined by F08FSF (CHETRD/ZHETRD)  |



- F08GCF All eigenvalues and optionally all eigenvectors of real symmetric matrix, packed storage, using divide and conquer
- F08GEF Orthogonal reduction of real symmetric matrix to symmetric tridiagonal form, packed storage
- F08GFF Generate orthogonal transformation matrix from reduction to tridiagonal form determined by F08GEF (SSPTRD/DSPTRD)
- F08GGF Apply orthogonal transformation determined by F08GEF (SSPTRD/DSPTRD)
- F08GQF All eigenvalues and optionally all eigenvectors of complex Hermitian matrix, packed storage, using divide and conquer
- F08GSF Unitary reduction of complex Hermitian matrix to real symmetric tridiagonal form, packed storage
- F08GTF Generate unitary transformation matrix from reduction to tridiagonal form determined by F08GSF (CHPTRD/ZHPTRD)
- F08GUF Apply unitary transformation matrix determined by F08GSF (CHPTRD/ZHPTRD)
- F08HCF All eigenvalues and optionally all eigenvectors of real symmetric band matrix, using divide and conquer
- F08HEF Orthogonal reduction of real symmetric band matrix to symmetric tridiagonal form
- F08HQF All eigenvalues and optionally all eigenvectors of complex Hermitian band matrix, using divide and conquer
- F08HSF Unitary reduction of complex Hermitian band matrix to real symmetric tridiagonal form
- F08JCF All eigenvalues and optionally all eigenvectors of real symmetric tridiagonal matrix, using divide and conquer
- F08JEF All eigenvalues and eigenvectors of real symmetric tridiagonal matrix, reduced from real symmetric matrix using implicit  $QL$  or  $QR$
- F08JFF All eigenvalues of real symmetric tridiagonal matrix, root-free variant of  $QL$  or  $QR$
- F08JGF All eigenvalues and eigenvectors of real symmetric positive-definite tridiagonal matrix, reduced from real symmetric positive-definite matrix
- F08JJF Selected eigenvalues of real symmetric tridiagonal matrix by bisection
- F08JKF Selected eigenvectors of real symmetric tridiagonal matrix by inverse iteration, storing eigenvectors in real array
- F08JSF All eigenvalues and eigenvectors of real symmetric tridiagonal matrix, reduced from complex Hermitian matrix, using implicit  $QL$  or  $QR$
- F08JUF All eigenvalues and eigenvectors of real symmetric positive-definite tridiagonal matrix, reduced from complex Hermitian positive-definite matrix
- F08JXF Selected eigenvectors of real symmetric tridiagonal matrix by inverse iteration, storing eigenvectors in complex array
- F08KEF Orthogonal reduction of real general rectangular matrix to bidiagonal form
- F08KFF Generate orthogonal transformation matrices from reduction to bidiagonal form determined by F08KEF (SGBRD/DGBRD)
- F08KGF Apply orthogonal transformations from reduction to bidiagonal form determined by F08KEF (SGBRD/DGBRD)
- F08KSF Unitary reduction of complex general rectangular matrix to bidiagonal form
- F08KTF Generate unitary transformation matrices from reduction to bidiagonal form determined by F08KSF (CGBRD/ZGBRD)
- F08KUF Apply unitary transformations from reduction to bidiagonal form determined by F08KSF (CGBRD/ZGBRD)
- F08LEF Reduction of real rectangular band matrix to upper bidiagonal form
- F08LSF Reduction of complex rectangular band matrix to upper bidiagonal form
- F08MEF SVD of real bidiagonal matrix reduced from real general matrix
- F08MSF SVD of real bidiagonal matrix reduced from complex general matrix
- F08NEF Orthogonal reduction of real general matrix to upper Hessenberg form
- F08NFF Generate orthogonal transformation matrix from reduction to Hessenberg form determined by F08NEF (SGEHRD/DGEHRD)
- F08NGF Apply orthogonal transformation matrix from reduction to Hessenberg form determined by F08NEF (SGEHRD/DGEHRD)
- F08NHF Balance real general matrix
- F08NJF Transform eigenvectors of real balanced matrix to those of original matrix supplied to F08NHF (SGBAL/DGBAL)
- F08NSF Unitary reduction of complex general matrix to upper Hessenberg form

- F08NTF Generate unitary transformation matrix from reduction to Hessenberg form determined by F08NSF (CGEHRD/ZGEHRD)
- F08NUF Apply unitary transformation matrix from reduction to Hessenberg form determined by F08NSF (CGEHRD/ZGEHRD)
- F08NVF Balance complex general matrix
- F08NWF Transform eigenvectors of complex balanced matrix to those of original matrix supplied to F08NVF (CGEBAL/ZGEBAL)
- F08PEF Eigenvalues and Schur factorization of real upper Hessenberg matrix reduced from real general matrix
- F08PKF Selected right and/or left eigenvectors of real upper Hessenberg matrix by inverse iteration
- F08PSF Eigenvalues and Schur factorization of complex upper Hessenberg matrix reduced from complex general matrix
- F08PXF Selected right and/or left eigenvectors of complex upper Hessenberg matrix by inverse iteration
- F08QFF Reorder Schur factorization of real matrix using orthogonal similarity transformation
- F08QGF Reorder Schur factorization of real matrix, form orthonormal basis of right invariant subspace for selected eigenvalues, with estimates of sensitivities
- F08QHF Solve real Sylvester matrix equation  $AX + XB = C$ ,  $A$  and  $B$  are upper quasi-triangular or transposes
- F08QKF Left and right eigenvectors of real upper quasi-triangular matrix
- F08QLF Estimates of sensitivities of selected eigenvalues and eigenvectors of real upper quasi-triangular matrix
- F08QTF Reorder Schur factorization of complex matrix using unitary similarity transformation
- F08QUF Reorder Schur factorization of complex matrix, form orthonormal basis of right invariant subspace for selected eigenvalues, with estimates of sensitivities
- F08QVF Solve complex Sylvester matrix equation  $AX + XB = C$ ,  $A$  and  $B$  are upper triangular or conjugate-transposes
- F08QXF Left and right eigenvectors of complex upper triangular matrix
- F08QYF Estimates of sensitivities of selected eigenvalues and eigenvectors of complex upper triangular matrix
- F08SEF Reduction to standard form of real symmetric-definite generalized eigenproblem  $Ax = \lambda Bx$ ,  $ABx = \lambda x$  or  $BAx = \lambda x$ ,  $B$  factorized by F07FDF (SPOTRF/DPOTRF)
- F08SSF Reduction to standard form of complex Hermitian-definite generalized eigenproblem  $Ax = \lambda Bx$ ,  $ABx = \lambda x$  or  $BAx = \lambda x$ ,  $B$  factorized by F07FRF (CPOTRF/ZPOTRF)
- F08TEF Reduction to standard form of real symmetric-definite generalized eigenproblem  $Ax = \lambda Bx$ ,  $ABx = \lambda x$  or  $BAx = \lambda x$ , packed storage,  $B$  factorized by F07GDF (SPPTRF/DPPTRF)
- F08TSF Reduction to standard form of complex Hermitian-definite generalized eigenproblem  $Ax = \lambda Bx$ ,  $ABx = \lambda x$  or  $BAx = \lambda x$ , packed storage,  $B$  factorized by F07GRF (CPPTRF/ZPPTRF)
- F08UEF Reduction of real symmetric-definite banded generalized eigenproblem  $Ax = \lambda Bx$  to standard form  $Cy = \lambda y$ , such that  $C$  has the same bandwidth as  $A$
- F08UFF Computes a split Cholesky factorization of real symmetric positive-definite band matrix  $A$
- F08USF Reduction of complex Hermitian-definite banded generalized eigenproblem  $Ax = \lambda Bx$  to standard form  $Cy = \lambda y$ , such that  $C$  has the same bandwidth as  $A$
- F08UTF Computes a split Cholesky factorization of complex Hermitian positive-definite band matrix  $A$
- F08WEF Orthogonal reduction of a pair of real general matrices to generalized upper Hessenberg form
- F08WHF Balance a pair of real general matrices
- F08WJF Transform eigenvectors of a pair of real balanced matrices to those of original matrix pair supplied to F08WHF (SGGBAL/DGGBAL)
- F08WSF Unitary reduction of a pair of complex general matrices to generalized upper Hessenberg form
- F08WVF Balance a pair of complex general matrices
- F08WWF Transform eigenvectors of a pair of complex balanced matrices to those of original matrix pair supplied to F08WVF (CGGBAL/ZGGBAL)
- F08XEF Eigenvalues and generalized Schur factorization of real generalized upper Hessenberg matrix reduced from a pair of real general matrices
- F08XSF Eigenvalues and generalized Schur factorization of complex generalized upper Hessenberg matrix reduced from a pair of complex general matrices
- F08YKF Left and right eigenvectors of a pair of real upper quasi-triangular matrices
- F08YXF Left and right eigenvectors of a pair of complex upper triangular matrices

**F11 – Sparse Linear Algebra**

- F11BAF Real sparse nonsymmetric linear systems, setup for F11BBF
- F11BBF Real sparse nonsymmetric linear systems, preconditioned RGMRES, CGS or Bi-CGSTAB
- F11BCF Real sparse nonsymmetric linear systems, diagnostic for F11BBF
- F11BDF Real sparse nonsymmetric linear systems, setup for F11BEF
- F11BEF Real sparse nonsymmetric linear systems, preconditioned RGMRES, CGS, Bi-CGSTAB or TFQMR method
- F11BFF Real sparse nonsymmetric linear systems, diagnostic for F11BEF
- F11BRF Complex sparse non-Hermitian linear systems, setup for F11BSF
- F11BSF Complex sparse non-Hermitian linear systems, preconditioned RGMRES, CGS, Bi-CGSTAB or TFQMR method
- F11BTF Complex sparse non-Hermitian linear systems, diagnostic for F11BSF
- F11DAF Real sparse nonsymmetric linear systems, incomplete *LU* factorization
- F11DBF Solution of linear system involving incomplete *LU* preconditioning matrix generated by F11DAF
- F11DCF Solution of real sparse nonsymmetric linear system, RGMRES, CGS, Bi-CGSTAB or TFQMR method, preconditioner computed by F11DAF
- F11DDF Solution of linear system involving preconditioning matrix generated by applying SSOR to real sparse nonsymmetric matrix
- F11DEF Solution of real sparse nonsymmetric linear system, RGMRES, CGS, Bi-CGSTAB, or TFQMR method, Jacobi or SSOR preconditioner (Black Box)
- F11DKF Real sparse nonsymmetric linear systems, line Jacobi preconditioner
- F11DNF Complex sparse non-Hermitian linear systems, incomplete *LU* factorization
- F11DPF Solution of complex linear system involving incomplete *LU* preconditioning matrix generated by F11DNF
- F11DQF Solution of complex sparse non-Hermitian linear system, RGMRES, CGS, Bi-CGSTAB or TFQMR method, preconditioner computed by F11DNF (Black Box)
- F11DRF Solution of linear system involving preconditioning matrix generated by applying SSOR to complex sparse non-Hermitian matrix
- F11DSF Solution of complex sparse non-Hermitian linear system, RGMRES, CGS, Bi-CGSTAB or TFQMR method, Jacobi or SSOR preconditioner Black Box
- F11DXF Complex sparse nonsymmetric linear systems, line Jacobi preconditioner
- F11GAF Real sparse symmetric linear systems, setup for F11GBF
- F11GBF Real sparse symmetric linear systems, preconditioned conjugate gradient or Lanczos
- F11GCF Real sparse symmetric linear systems, diagnostic for F11GBF
- F11GDF Real sparse symmetric linear systems, setup for F11GEF
- F11GEF Real sparse symmetric linear systems, preconditioned conjugate gradient or Lanczos
- F11GFF Real sparse symmetric linear systems, diagnostic for F11GEF
- F11GRF Complex sparse symmetric linear systems, setup for F11GEF
- F11GSF Complex sparse symmetric linear systems, preconditioned conjugate gradient or Lanczos
- F11GTF Complex sparse symmetric linear systems, diagnostic for F11GEF
- F11JAF Real sparse symmetric matrix, incomplete Cholesky factorization
- F11JBF Solution of linear system involving incomplete Cholesky preconditioning matrix generated by F11JAF
- F11JCF Solution of real sparse symmetric linear system, conjugate gradient/Lanczos method, preconditioner computed by F11JAF (Black Box)
- F11JDF Solution of linear system involving preconditioning matrix generated by applying SSOR to real sparse symmetric matrix
- F11JEF Solution of real sparse symmetric linear system, conjugate gradient/Lanczos method, Jacobi or SSOR preconditioner (Black Box)
- F11JNF Complex sparse Hermitian matrix, incomplete Cholesky factorization
- F11JPF Solution of complex linear system involving incomplete Cholesky preconditioning matrix generated by F11JNF
- F11JQF Solution of complex sparse Hermitian linear system, conjugate gradient/Lanczos method, preconditioner computed by F11JNF (Black Box)
- F11JRF Solution of linear system involving preconditioning matrix generated by applying SSOR to complex sparse Hermitian matrix

|        |  |
|--------|--|
| F11JSF | Solution of complex sparse Hermitian linear system, conjugate gradient/Lanczos method, Jacobi or SSOR preconditioner (Black Box) |
| F11XAF | Real sparse nonsymmetric matrix vector multiply  |
| F11XEF | Real sparse symmetric matrix vector multiply   |
| F11XNF | Complex sparse non-Hermitian matrix vector multiply  |
| F11XSF | Complex sparse Hermitian matrix vector multiply  |
| F11ZAF | Real sparse nonsymmetric matrix reorder routine  |
| F11ZBF | Real sparse symmetric matrix reorder routine   |
| F11ZNF | Complex sparse non-Hermitian matrix reorder routine  |
| F11ZPF | Complex sparse Hermitian matrix reorder routine  |

## G01 – Simple Calculations on Statistical Data

|        |  |
|--------|--|
| G01AAF | Mean, variance, skewness, kurtosis, etc, one variable, from raw data                                   |
| G01ABF | Mean, variance, skewness, kurtosis, etc, two variables, from raw data                                  |
| G01ADF | Mean, variance, skewness, kurtosis, etc, one variable, from frequency table                            |
| G01AEF | Frequency table from raw data  |
| G01AFF | Two-way contingency table analysis, with $\chi^2$ /Fisher's exact test                                 |
| G01AGF | Lineprinter scatterplot of two variables   |
| G01AHF | Lineprinter scatterplot of one variable against Normal scores  |
| G01AJF | Lineprinter histogram of one variable  |
| G01ALF | Computes a five-point summary (median, hinges and extremes)  |
| G01ARF | Constructs a stem and leaf plot  |
| G01ASF | Constructs a box and whisker plot  |
| G01BJF | Binomial distribution function   |
| G01BKF | Poisson distribution function  |
| G01BLF | Hypergeometric distribution function   |
| G01DAF | Normal scores, accurate values   |
| G01DBF | Normal scores, approximate values  |
| G01DCF | Normal scores, approximate variance-covariance matrix  |
| G01DDF | Shapiro and Wilk's $W$ test for Normality  |
| G01DHF | Ranks, Normal scores, approximate Normal scores or exponential (Savage) scores                         |
| G01EAF | Computes probabilities for the standard Normal distribution  |
| G01EBF | Computes probabilities for Student's $t$ -distribution   |
| G01ECF | Computes probabilities for $\chi^2$ distribution   |
| G01EDF | Computes probabilities for $F$ -distribution   |
| G01EEF | Computes upper and lower tail probabilities and probability density function for the beta distribution |
| G01EFF | Computes probabilities for the gamma distribution  |
| G01EMF | Computes probability for the Studentized range statistic   |
| G01EPF | Computes bounds for the significance of a Durbin-Watson statistic                                      |
| G01ERF | Computes probability for von Mises distribution  |
| G01EYF | Computes probabilities for the one-sample Kolmogorov-Smirnov distribution                              |
| G01EZF | Computes probabilities for the two-sample Kolmogorov-Smirnov distribution                              |
| G01FAF | Computes deviates for the standard Normal distribution   |
| G01FBF | Computes deviates for Student's $t$ -distribution  |
| G01FCF | Computes deviates for the $\chi^2$ distribution  |
| G01FDF | Computes deviates for the $F$ -distribution  |
| G01FEF | Computes deviates for the beta distribution  |
| G01FFF | Computes deviates for the gamma distribution   |
| G01FMF | Computes deviates for the Studentized range statistic  |
| G01GBF | Computes probabilities for the non-central Student's $t$ -distribution                                 |
| G01GCF | Computes probabilities for the non-central $\chi^2$ distribution                                       |
| G01GDF | Computes probabilities for the non-central $F$ -distribution   |
| G01GEF | Computes probabilities for the non-central beta distribution   |
| G01HAF | Computes probability for the bivariate Normal distribution   |
| G01HBF | Computes probabilities for the multivariate Normal distribution  |
| G01JCF | Computes probability for a positive linear combination of $\chi^2$ variables                           |

- G01JDF Computes lower tail probability for a linear combination of (central)  $\chi^2$  variables  
 G01MBF Computes reciprocal of Mills' Ratio  
 G01NAF Cumulants and moments of quadratic forms in Normal variables  
 G01NBF Moments of ratios of quadratic forms in Normal variables, and related statistics

## G02 – Correlation and Regression Analysis

- G02BAF Pearson product-moment correlation coefficients, all variables, no missing values  
 G02BBF Pearson product-moment correlation coefficients, all variables, casewise treatment of missing values  
 G02BCF Pearson product-moment correlation coefficients, all variables, pairwise treatment of missing values  
 G02BDF Correlation-like coefficients (about zero), all variables, no missing values  
 G02BEF Correlation-like coefficients (about zero), all variables, casewise treatment of missing values  
 G02BFF Correlation-like coefficients (about zero), all variables, pairwise treatment of missing values  
 G02BGF Pearson product-moment correlation coefficients, subset of variables, no missing values  
 G02BHF Pearson product-moment correlation coefficients, subset of variables, casewise treatment of missing values  
 G02BJF Pearson product-moment correlation coefficients, subset of variables, pairwise treatment of missing values  
 G02BKF Correlation-like coefficients (about zero), subset of variables, no missing values  
 G02BLF Correlation-like coefficients (about zero), subset of variables, casewise treatment of missing values  
 G02BMF Correlation-like coefficients (about zero), subset of variables, pairwise treatment of missing values  
 G02BNF Kendall/Spearman non-parametric rank correlation coefficients, no missing values, overwriting input data  
 G02BPF Kendall/Spearman non-parametric rank correlation coefficients, casewise treatment of missing values, overwriting input data  
 G02BQF Kendall/Spearman non-parametric rank correlation coefficients, no missing values, preserving input data  
 G02BRF Kendall/Spearman non-parametric rank correlation coefficients, casewise treatment of missing values, preserving input data  
 G02BSF Kendall/Spearman non-parametric rank correlation coefficients, pairwise treatment of missing values  
 G02BTF Update a weighted sum of squares matrix with a new observation  
 G02BUF Computes a weighted sum of squares matrix  
 G02BWF Computes a correlation matrix from a sum of squares matrix  
 G02BXF Computes (optionally weighted) correlation and covariance matrices  
 G02BYF Computes partial correlation/variance-covariance matrix from correlation/variance-covariance matrix computed by G02BXF  
 G02CAF Simple linear regression with constant term, no missing values  
 G02CBF Simple linear regression without constant term, no missing values  
 G02CCF Simple linear regression with constant term, missing values  
 G02CDF Simple linear regression without constant term, missing values  
 G02CEF Service routines for multiple linear regression, select elements from vectors and matrices  
 G02CFF Service routines for multiple linear regression, re-order elements of vectors and matrices  
 G02CGF Multiple linear regression, from correlation coefficients, with constant term  
 G02CHF Multiple linear regression, from correlation-like coefficients, without constant term  
 G02DAF Fits a general (multiple) linear regression model  
 G02DCF Add/delete an observation to/from a general linear regression model  
 G02DDF Estimates of linear parameters and general linear regression model from updated model  
 G02DEF Add a new variable to a general linear regression model  
 G02DFF Delete a variable from a general linear regression model  
 G02DGF Fits a general linear regression model for new dependent variable  
 G02DKF Estimates and standard errors of parameters of a general linear regression model for given constraints  
 G02DNF Computes estimable function of a general linear regression model and its standard error

- G02EAF Computes residual sums of squares for all possible linear regressions for a set of independent variables
- G02ECF Calculates  $R^2$  and  $C_P$  values from residual sums of squares
- G02EEF Fits a linear regression model by forward selection
- G02FAF Calculates standardized residuals and influence statistics
- G02FCF Computes Durbin–Watson test statistic
- G02GAF Fits a generalized linear model with Normal errors
- G02GBF Fits a generalized linear model with binomial errors
- G02GCF Fits a generalized linear model with Poisson errors
- G02GDF Fits a generalized linear model with gamma errors
- G02GKF Estimates and standard errors of parameters of a general linear model for given constraints
- G02GNF Computes estimable function of a generalized linear model and its standard error
- G02HAF Robust regression, standard  $M$ -estimates
- G02HBF Robust regression, compute weights for use with G02HDF
- G02HDF Robust regression, compute regression with user-supplied functions and weights
- G02HFF Robust regression, variance-covariance matrix following G02HDF
- G02HKF Calculates a robust estimation of a correlation matrix, Huber’s weight function
- G02HLF Calculates a robust estimation of a correlation matrix, user-supplied weight function plus derivatives
- G02HMF Calculates a robust estimation of a correlation matrix, user-supplied weight function

### G03 – Multivariate Methods

- G03AAF Performs principal component analysis
- G03ACF Performs canonical variate analysis
- G03ADF Performs canonical correlation analysis
- G03BAF Computes orthogonal rotations for loading matrix, generalized orthomax criterion
- G03BCF Computes Procrustes rotations
- G03CAF Computes maximum likelihood estimates of the parameters of a factor analysis model, factor loadings, communalities and residual correlations
- G03CCF Computes factor score coefficients (for use after G03CAF)
- G03DAF Computes test statistic for equality of within-group covariance matrices and matrices for discriminant analysis
- G03DBF Computes Mahalanobis squared distances for group or pooled variance-covariance matrices (for use after G03DAF)
- G03DCF Allocates observations to groups according to selected rules (for use after G03DAF)
- G03EAF Computes distance matrix
- G03ECF Hierarchical cluster analysis
- G03EFF  $K$ -means cluster analysis
- G03EHF Constructs dendrogram (for use after G03ECF)
- G03EJF Computes cluster indicator variable (for use after G03ECF)
- G03FAF Performs principal co-ordinate analysis, classical metric scaling
- G03FCF Performs non-metric (ordinal) multidimensional scaling
- G03ZAF Produces standardized values ( $z$ -scores) for a data matrix

### G04 – Analysis of Variance

- G04AGF Two-way analysis of variance, hierarchical classification, subgroups of unequal size
- G04BBF Analysis of variance, randomized block or completely randomized design, treatment means and standard errors
- G04BCF Analysis of variance, general row and column design, treatment means and standard errors
- G04CAF Analysis of variance, complete factorial design, treatment means and standard errors
- G04DAF Computes sum of squares for contrast between means
- G04DBF Computes confidence intervals for differences between means computed by G04BBF or G04BCF,
- G04EAF Computes orthogonal polynomials or dummy variables for factor/classification variable

**G05 – Random Number Generators**

- G05CAF Pseudo-random real numbers, uniform distribution over (0,1)
- G05CBF Initialise random number generating routines to give repeatable sequence
- G05CCF Initialise random number generating routines to give non-repeatable sequence
- G05CFF Save state of random number generating routines
- G05CGF Restore state of random number generating routines
- G05DAF Pseudo-random real numbers, uniform distribution over  $(a, b)$
- G05DBF Pseudo-random real numbers, (negative) exponential distribution
- G05DCF Pseudo-random real numbers, logistic distribution
- G05DDF Pseudo-random real numbers, Normal distribution
- G05DEF Pseudo-random real numbers, log-normal distribution
- G05DFF Pseudo-random real numbers, Cauchy distribution
- G05DHF Pseudo-random real numbers,  $\chi^2$  distribution
- G05DJF Pseudo-random real numbers, Student's  $t$ -distribution
- G05DKF Pseudo-random real numbers,  $F$ -distribution
- G05DPF Pseudo-random real numbers, Weibull distribution
- G05DRF Pseudo-random integer, Poisson distribution
- G05DYF Pseudo-random integer from uniform distribution
- G05DZF Pseudo-random logical (boolean) value
- G05EAF Set up reference vector for multivariate Normal distribution
- G05EBF Set up reference vector for generating pseudo-random integers, uniform distribution
- G05ECF Set up reference vector for generating pseudo-random integers, Poisson distribution
- G05EDF Set up reference vector for generating pseudo-random integers, binomial distribution
- G05EEF Set up reference vector for generating pseudo-random integers, negative binomial distribution
- G05EFF Set up reference vector for generating pseudo-random integers, hypergeometric distribution
- G05EGF Set up reference vector for univariate ARMA time series model
- G05EHF Pseudo-random permutation of an integer vector
- G05EJF Pseudo-random sample from an integer vector
- G05EWF Generate next term from reference vector for ARMA time series model
- G05EXF Set up reference vector from supplied cumulative distribution function or probability distribution function
- G05EYF Pseudo-random integer from reference vector
- G05EZF Pseudo-random multivariate Normal vector from reference vector
- G05FAF Generates a vector of random numbers from a uniform distribution
- G05FBF Generates a vector of random numbers from an (negative) exponential distribution
- G05FDF Generates a vector of random numbers from a Normal distribution
- G05FEF Generates a vector of pseudo-random numbers from a beta distribution
- G05FFF Generates a vector of pseudo-random numbers from a gamma distribution
- G05FSF Generates a vector of pseudo-random variates from von Mises distribution
- G05GAF Computes a random orthogonal matrix
- G05GBF Computes a random correlation matrix
- G05HDF Generates a realisation of a multivariate time series from a VARMA model
- G05HKF Univariate time series, generate  $n$  terms of either a symmetric GARCH process or a GARCH process with asymmetry of the form  $(\epsilon_{t-1} + \gamma)^2$
- G05HLF Univariate time series, generate  $n$  terms of a GARCH process with asymmetry of the form  $(|\epsilon_{t-1}| + \gamma\epsilon_{t-1})^2$
- G05HMF Univariate time series, generate  $n$  terms of an asymmetric Glosten, Jagannathan and Runkle (GJR) GARCH process
- G05HNF Univariate time series, generate  $n$  terms of an exponential GARCH (EGARCH) process
- G05KAF Pseudo-random real numbers, uniform distribution over (0,1), seeds and generator number passed explicitly
- G05KBF Initialise seeds of a given generator for random number generating routines (that pass seeds explicitly) to give a repeatable sequence
- G05KCF Initialise seeds of a given generator for random number generating routines (that pass seeds explicitly) to give non-repeatable sequence
- G05KEF Pseudo-random logical (boolean) value, seeds and generator number passed explicitly
- G05LAF Generates a vector of random numbers from a Normal distribution, seeds and generator number passed explicitly

|        |   |
|--------|---|
| G05LBF | Generates a vector of random numbers from a Student's $t$ -distribution, seeds and generator number passed explicitly             |
| G05LCF | Generates a vector of random numbers from a $\chi^2$ distribution, seeds and generator number passed explicitly                   |
| G05LDF | Generates a vector of random numbers from an $F$ -distribution, seeds and generator number passed explicitly                      |
| G05LEF | Generates a vector of random numbers from a $\beta$ distribution, seeds and generator number passed explicitly                    |
| G05LFF | Generates a vector of random numbers from a $\gamma$ distribution, seeds and generator number passed explicitly                   |
| G05LGF | Generates a vector of random numbers from a uniform distribution, seeds and generator number passed explicitly                    |
| G05LHF | Generates a vector of random numbers from a triangular distribution, seeds and generator number passed explicitly                 |
| G05LJF | Generates a vector of random numbers from an exponential distribution, seeds and generator number passed explicitly               |
| G05LKF | Generates a vector of random numbers from a lognormal distribution, seeds and generator number passed explicitly                  |
| G05LLF | Generates a vector of random numbers from a Cauchy distribution, seeds and generator number passed explicitly                     |
| G05LMF | Generates a vector of random numbers from a Weibull distribution, seeds and generator number passed explicitly                    |
| G05LNF | Generates a vector of random numbers from a logistic distribution, seeds and generator number passed explicitly                   |
| G05LPF | Generates a vector of random numbers from a Von Mises distribution, seeds and generator number passed explicitly                  |
| G05LQF | Generates a vector of random numbers from an exponential mixture distribution, seeds and generator number passed explicitly       |
| G05LZF | Generates a vector of random numbers from a multivariate Normal distribution, seeds and generator number passed explicitly        |
| G05MAF | Generates a vector of random integers from a uniform distribution, seeds and generator number passed explicitly                   |
| G05MBF | Generates a vector of random integers from a geometric distribution, seeds and generator number passed explicitly                 |
| G05MCF | Generates a vector of random integers from a negative binomial distribution, seeds and generator number passed explicitly         |
| G05MDF | Generates a vector of random integers from a logarithmic distribution, seeds and generator number passed explicitly               |
| G05MEF | Generates a vector of random integers from a Poisson distribution with varying mean, seeds and generator number passed explicitly |
| G05MJF | Generates a vector of random integers from a binomial distribution, seeds and generator number passed explicitly                  |
| G05MKF | Generates a vector of random integers from a Poisson distribution, seeds and generator number passed explicitly                   |
| G05MLF | Generates a vector of random integers from a hypergeometric distribution, seeds and generator number passed explicitly            |
| G05MRF | Generates a vector of random integers from a multinomial distribution, seeds and generator number passed explicitly               |
| G05MZF | Generates a vector of random integers from a general discrete distribution, seeds and generator number passed explicitly          |
| G05NAF | Pseudo-random permutation of an integer vector  |
| G05NBF | Pseudo-random sample from an integer vector   |
| G05PAF | Generates a realisation of a time series from an ARMA model   |
| G05PCF | Generates a realisation of a multivariate time series from a VARMA model  |
| G05QAF | Computes a random orthogonal matrix   |
| G05QBF | Computes a random correlation matrix  |
| G05QDF | Generates a random table matrix   |
| G05YAF | Multi-dimensional quasi-random number generator with a uniform probability distribution   |



- G05YBF Multi-dimensional quasi-random number generator with a Gaussian or log-normal probability distribution
- G05ZAF Selects either the basic generator or the Wichmann–Hill generator for those routines using internal communication

### **G07 – Univariate Estimation**

- G07AAF Computes confidence interval for the parameter of a binomial distribution
- G07ABF Computes confidence interval for the parameter of a Poisson distribution
- G07BBF Computes maximum likelihood estimates for parameters of the Normal distribution from grouped and/or censored data
- G07BEF Computes maximum likelihood estimates for parameters of the Weibull distribution
- G07CAF Computes  $t$ -test statistic for a difference in means between two Normal populations, confidence interval
- G07DAF Robust estimation, median, median absolute deviation, robust standard deviation
- G07DBF Robust estimation,  $M$ -estimates for location and scale parameters, standard weight functions
- G07DCF Robust estimation,  $M$ -estimates for location and scale parameters, user-defined weight functions
- G07DDF Computes a trimmed and winsorized mean of a single sample with estimates of their variance
- G07EAF Robust confidence intervals, one-sample
- G07EBF Robust confidence intervals, two-sample

### **G08 – Nonparametric Statistics**

- G08AAF Sign test on two paired samples
- G08ACF Median test on two samples of unequal size
- G08AEF Friedman two-way analysis of variance on  $k$  matched samples
- G08AFF Kruskal–Wallis one-way analysis of variance on  $k$  samples of unequal size
- G08AGF Performs the Wilcoxon one-sample (matched pairs) signed rank test
- G08AHF Performs the Mann–Whitney  $U$  test on two independent samples
- G08AJF Computes the exact probabilities for the Mann–Whitney  $U$  statistic, no ties in pooled sample
- G08AKF Computes the exact probabilities for the Mann–Whitney  $U$  statistic, ties in pooled sample
- G08ALF Performs the Cochran  $Q$  test on cross-classified binary data
- G08BAF Mood’s and David’s tests on two samples of unequal size
- G08CBF Performs the one-sample Kolmogorov–Smirnov test for standard distributions
- G08CCF Performs the one-sample Kolmogorov–Smirnov test for a user-supplied distribution
- G08CDF Performs the two-sample Kolmogorov–Smirnov test
- G08CGF Performs the  $\chi^2$  goodness of fit test, for standard continuous distributions
- G08DAF Kendall’s coefficient of concordance
- G08EAF Performs the runs up or runs down test for randomness
- G08EBF Performs the pairs (serial) test for randomness
- G08ECF Performs the triplets test for randomness
- G08EDF Performs the gaps test for randomness
- G08RAF Regression using ranks, uncensored data
- G08RBF Regression using ranks, right-censored data

### **G10 – Smoothing in Statistics**

- G10ABF Fit cubic smoothing spline, smoothing parameter given
- G10ACF Fit cubic smoothing spline, smoothing parameter estimated
- G10BAF Kernel density estimate using Gaussian kernel
- G10CAF Compute smoothed data sequence using running median smoothers
- G10ZAF Reorder data to give ordered distinct observations

### **G11 – Contingency Table Analysis**

- G11AAF  $\chi^2$  statistics for two-way contingency table
- G11BAF Computes multiway table from set of classification factors using selected statistic
- G11BBF Computes multiway table from set of classification factors using given percentile/quantile
- G11BCF Computes marginal tables for multiway table computed by G11BAF or G11BBF

- G11CAF Returns parameter estimates for the conditional analysis of stratified data
- G11SAF Contingency table, latent variable model for binary data
- G11SBF Frequency count for G11SAF

## G12 – Survival Analysis

- G12AAF Computes Kaplan–Meier (product-limit) estimates of survival probabilities
- G12BAF Fits Cox’s proportional hazard model
- G12ZAF Creates the risk sets associated with the Cox proportional hazards model for fixed covariates

## G13 – Time Series Analysis

- G13AAF Univariate time series, seasonal and non-seasonal differencing
- G13ABF Univariate time series, sample autocorrelation function
- G13ACF Univariate time series, partial autocorrelations from autocorrelations
- G13ADF Univariate time series, preliminary estimation, seasonal ARIMA model
- G13AEF Univariate time series, estimation, seasonal ARIMA model (comprehensive)
- G13AFF Univariate time series, estimation, seasonal ARIMA model (easy-to-use)
- G13AGF Univariate time series, update state set for forecasting
- G13AHF Univariate time series, forecasting from state set
- G13AJF Univariate time series, state set and forecasts, from fully specified seasonal ARIMA model
- G13ASF Univariate time series, diagnostic checking of residuals, following G13AEF or G13AFF
- G13AUF Computes quantities needed for range-mean or standard deviation-mean plot
- G13BAF Multivariate time series, filtering (pre-whitening) by an ARIMA model
- G13BBF Multivariate time series, filtering by a transfer function model
- G13BCF Multivariate time series, cross-correlations
- G13BDF Multivariate time series, preliminary estimation of transfer function model
- G13BEF Multivariate time series, estimation of multi-input model
- G13BGF Multivariate time series, update state set for forecasting from multi-input model
- G13BHF Multivariate time series, forecasting from state set of multi-input model
- G13BJF Multivariate time series, state set and forecasts from fully specified multi-input model
- G13CAF Univariate time series, smoothed sample spectrum using rectangular, Bartlett, Tukey or Parzen lag window
- G13CBF Univariate time series, smoothed sample spectrum using spectral smoothing by the trapezium frequency (Daniell) window
- G13CCF Multivariate time series, smoothed sample cross spectrum using rectangular, Bartlett, Tukey or Parzen lag window
- G13CDF Multivariate time series, smoothed sample cross spectrum using spectral smoothing by the trapezium frequency (Daniell) window
- G13CEF Multivariate time series, cross amplitude spectrum, squared coherency, bounds, univariate and bivariate (cross) spectra
- G13CFE Multivariate time series, gain, phase, bounds, univariate and bivariate (cross) spectra
- G13CGF Multivariate time series, noise spectrum, bounds, impulse response function and its standard error
- G13DBF Multivariate time series, multiple squared partial autocorrelations
- G13DCF Multivariate time series, estimation of VARMA model
- G13DJF Multivariate time series, forecasts and their standard errors
- G13DKF Multivariate time series, updates forecasts and their standard errors
- G13DLF Multivariate time series, differences and/or transforms (for use before G13DCF)
- G13DMF Multivariate time series, sample cross-correlation or cross-covariance matrices
- G13DNF Multivariate time series, sample partial lag correlation matrices,  $\chi^2$  statistics and significance levels
- G13DPF Multivariate time series, partial autoregression matrices
- G13DSF Multivariate time series, diagnostic checking of residuals, following G13DCF
- G13DXF Calculates the zeros of a vector autoregressive (or moving average) operator
- G13EAF Combined measurement and time update, one iteration of Kalman filter, time-varying, square root covariance filter
- G13EBF Combined measurement and time update, one iteration of Kalman filter, time-invariant, square root covariance filter

- G13FAF Univariate time series, parameter estimation for either a symmetric GARCH process or a GARCH process with asymmetry of the form  $(\epsilon_{t-1} + \gamma)^2$
- G13FBF Univariate time series, forecast function for either a symmetric GARCH process or a GARCH process with asymmetry of the form  $(\epsilon_{t-1} + \gamma)^2$
- G13FCF Univariate time series, parameter estimation for a GARCH process with asymmetry of the form  $(|\epsilon_{t-1}| + \gamma\epsilon_{t-1})^2$
- G13FDF Univariate time series, forecast function for a GARCH process with asymmetry of the form  $(|\epsilon_{t-1}| + \gamma\epsilon_{t-1})^2$
- G13FEF Univariate time series, parameter estimation for an asymmetric Glosten, Jagannathan and Runkle (GJR) GARCH process
- G13FFF Univariate time series, forecast function for an asymmetric Glosten, Jagannathan and Runkle (GJR) GARCH process
- G13FGF Univariate time series, forecast function for an exponential GARCH (EGARCH) process
- G13FHF Univariate time series, forecast function for an exponential GARCH (EGARCH) process

## H – Operations Research

- H02BBF Integer LP problem (dense)
- H02BFF Interpret MPSX data file defining IP or LP problem, optimize and print solution
- H02BUF Convert MPSX data file defining IP or LP problem to format required by H02BBF or E04MFF/E04MFA
- H02BVF Print IP or LP solutions with user specified names for rows and columns
- H02BZF Integer programming solution, supplies further information on solution obtained by H02BBF
- H02CBF Integer QP problem (dense)
- H02CCF Read optional parameter values for H02CBF from external file
- H02CDF Supply optional parameter values to H02CBF
- H02CEF Integer LP or QP problem (sparse)
- H02CFF Read optional parameter values for H02CEF from external file
- H02CGF Supply optional parameter values to H02CEF
- H03ABF Transportation problem, modified ‘stepping stone’ method
- H03ADF Shortest path problem, Dijkstra’s algorithm

## M01 – Sorting

- M01CAF Sort a vector, real numbers
- M01CBF Sort a vector, integer numbers
- M01CCF Sort a vector, character data
- M01DAF Rank a vector, real numbers
- M01DBF Rank a vector, integer numbers
- M01DCF Rank a vector, character data
- M01DEF Rank rows of a matrix, real numbers
- M01DFF Rank rows of a matrix, integer numbers
- M01DJF Rank columns of a matrix, real numbers
- M01DKF Rank columns of a matrix, integer numbers
- M01DZF Rank arbitrary data
- M01EAF Rearrange a vector according to given ranks, real numbers
- M01EBF Rearrange a vector according to given ranks, integer numbers
- M01ECF Rearrange a vector according to given ranks, character data
- M01EDF Rearrange a vector according to given ranks, complex numbers
- M01ZAF Invert a permutation
- M01ZBF Check validity of a permutation
- M01ZCF Decompose a permutation into cycles

## P01 – Error Trapping

- P01ABF Return value of error indicator/terminate with error message

**S – Approximations of Special Functions**

|        |   |
|--------|---|
| S01BAF | $\ln(1+x)$  |
| S01EAF | Complex exponential, $e^z$  |
| S07AAF | $\tan x$  |
| S09AAF | $\arcsin x$   |
| S09ABF | $\arccos x$   |
| S10AAF | $\tanh x$   |
| S10ABF | $\sinh x$   |
| S10ACF | $\cosh x$   |
| S11AAF | $\operatorname{arctanh} x$  |
| S11ABF | $\operatorname{arsinh} x$   |
| S11ACF | $\operatorname{arcosh} x$   |
| S13AAF | Exponential integral $E_1(x)$   |
| S13ACF | Cosine integral $\operatorname{Ci}(x)$  |
| S13ADF | Sine integral $\operatorname{Si}(x)$  |
| S14AAF | Gamma function  |
| S14ABF | Log Gamma function  |
| S14ACF | $\psi(x) - \ln x$   |
| S14ADF | Scaled derivatives of $\psi(x)$   |
| S14AEF | Polygamma function $\psi^{(n)}(x)$ for real $x$   |
| S14AFF | Polygamma function $\psi^{(n)}(z)$ for complex $z$  |
| S14BAF | Incomplete Gamma functions $P(a, x)$ and $Q(a, x)$  |
| S15ABF | Cumulative Normal distribution function $P(x)$  |
| S15ACF | Complement of cumulative Normal distribution function $Q(x)$  |
| S15ADF | Complement of error function $\operatorname{erfc}(x)$   |
| S15AEF | Error function $\operatorname{erf}(x)$  |
| S15AFF | Dawson's integral   |
| S15DDF | Scaled complex complement of error function, $\exp(-z^2)\operatorname{erfc}(-iz)$                           |
| S17ACF | Bessel function $Y_0(x)$  |
| S17ADF | Bessel function $Y_1(x)$  |
| S17AEF | Bessel function $J_0(x)$  |
| S17AFF | Bessel function $J_1(x)$  |
| S17AGF | Airy function $\operatorname{Ai}(x)$  |
| S17AHF | Airy function $\operatorname{Bi}(x)$  |
| S17AJF | Airy function $\operatorname{Ai}'(x)$   |
| S17AKF | Airy function $\operatorname{Bi}'(x)$   |
| S17ALF | Zeros of Bessel functions $J_\alpha(x)$ , $J'_\alpha(x)$ , $Y_\alpha(x)$ or $Y'_\alpha(x)$                  |
| S17DCF | Bessel functions $Y_{\nu+a}(z)$ , real $a \geq 0$ , complex $z$ , $\nu = 0, 1, 2, \dots$                    |
| S17DEF | Bessel functions $J_{\nu+a}(z)$ , real $a \geq 0$ , complex $z$ , $\nu = 0, 1, 2, \dots$                    |
| S17DGF | Airy functions $\operatorname{Ai}(z)$ and $\operatorname{Ai}'(z)$ , complex $z$                             |
| S17DHF | Airy functions $\operatorname{Bi}(z)$ and $\operatorname{Bi}'(z)$ , complex $z$                             |
| S17DLF | Hankel functions $H_{\nu+a}^{(j)}(z)$ , $j = 1, 2$ , real $a \geq 0$ , complex $z$ , $\nu = 0, 1, 2, \dots$ |
| S18ACF | Modified Bessel function $K_0(x)$   |
| S18ADF | Modified Bessel function $K_1(x)$   |
| S18AEF | Modified Bessel function $I_0(x)$   |
| S18AFF | Modified Bessel function $I_1(x)$   |
| S18CCF | Modified Bessel function $e^x K_0(x)$   |
| S18CDF | Modified Bessel function $e^x K_1(x)$   |
| S18CEF | Modified Bessel function $e^{- x } I_0(x)$  |
| S18CFF | Modified Bessel function $e^{- x } I_1(x)$  |
| S18DCF | Modified Bessel functions $K_{\nu+a}(z)$ , real $a \geq 0$ , complex $z$ , $\nu = 0, 1, 2, \dots$           |
| S18DEF | Modified Bessel functions $I_{\nu+a}(z)$ , real $a \geq 0$ , complex $z$ , $\nu = 0, 1, 2, \dots$           |
| S19AAF | Kelvin function $\operatorname{ber} x$  |
| S19ABF | Kelvin function $\operatorname{bei} x$  |
| S19ACF | Kelvin function $\operatorname{ker} x$  |
| S19ADF | Kelvin function $\operatorname{kei} x$  |
| S20ACF | Fresnel integral $S(x)$   |

|        |  |
|--------|--|
| S20ADF | Fresnel integral $C(x)$  |
| S21BAF | Degenerate symmetrised elliptic integral of 1st kind $R_C(x, y)$           |
| S21BBF | Symmetrised elliptic integral of 1st kind $R_F(x, y, z)$                   |
| S21BCF | Symmetrised elliptic integral of 2nd kind $R_D(x, y, z)$                   |
| S21BDF | Symmetrised elliptic integral of 3rd kind $R_J(x, y, z, r)$                |
| S21CAF | Jacobian elliptic functions sn, cn and dn of real argument                 |
| S21CBF | Jacobian elliptic functions sn, cn and dn of complex argument              |
| S21CCF | Jacobian theta functions $\theta_k(x, q)$ of real argument                 |
| S21DAF | General elliptic integral of 2nd kind $F(z, k', a, b)$ of complex argument |
| S22AAF | Legendre functions of 1st kind $P_n^m(x)$ or $\overline{P}_n^m(x)$         |

### X01 – Mathematical Constants

|        |  |
|--------|--|
| X01AAF | Provides the mathematical constant $\pi$                       |
| X01ABF | Provides the mathematical constant $\gamma$ (Euler's Constant) |

### X02 – Machine Constants

|        |  |
|--------|--|
| X02AHF | The largest permissible argument for sin and cos               |
| X02AJF | The machine precision  |
| X02AKF | The smallest positive model number                             |
| X02ALF | The largest positive model number                              |
| X02AMF | Safe range of real floating-point arithmetic                   |
| X02ANF | The safe range parameter for complex floating-point arithmetic |
| X02BBF | The largest representable integer                              |
| X02BEF | The maximum number of decimal digits that can be represented   |
| X02BHF | The floating-point model parameter, $b$                        |
| X02BJF | The floating-point model parameter, $p$                        |
| X02BKF | The floating-point model parameter $e_{\min}$                  |
| X02BLF | The floating-point model parameter $e_{\max}$                  |
| X02DAF | Switch for taking precautions to avoid underflow               |
| X02DJF | The floating-point model parameter ROUNDS                      |

### X03 – Inner Products

|        |  |
|--------|--|
| X03AAF | Real inner product added to initial value, basic/additional precision    |
| X03ABF | Complex inner product added to initial value, basic/additional precision |

### X04 – Input/Output Utilities

|        |  |
|--------|--|
| X04AAF | Returns or sets unit number for error message  |
| X04ABF | Returns or sets unit number for advisory message                                       |
| X04ACF | Open unit number for reading, writing or appending, and associate unit with named file |
| X04ADF | Close file associated with given unit number   |
| X04BAF | Write formatted record to external file  |
| X04BBF | Read formatted record from external file   |
| X04CAF | Print real general matrix (easy-to-use)  |
| X04CBF | Print real general matrix (comprehensive)  |
| X04CCF | Print real packed triangular matrix (easy-to-use)                                      |
| X04CDF | Print real packed triangular matrix (comprehensive)                                    |
| X04CEF | Print real packed banded matrix (easy-to-use)  |
| X04CFF | Print real packed banded matrix (comprehensive)  |
| X04DAF | Print complex general matrix (easy-to-use)   |
| X04DBF | Print complex general matrix (comprehensive)   |
| X04DCF | Print complex packed triangular matrix (easy-to-use)                                   |
| X04DDF | Print complex packed triangular matrix (comprehensive)                                 |
| X04DEF | Print complex packed banded matrix (easy-to-use)                                       |
| X04DFE | Print complex packed banded matrix (comprehensive)                                     |
| X04EAF | Print integer matrix (easy-to-use)   |